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Stiffening effects-controlling sizing procedure of ADAS dampers in seismic retrofit of frame structures

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Added Damping and Stiffness (ADAS) steel dissipators are among the most classical devices installed in dissipative bracing systems for the advanced seismic retrofit of frame buildings. An energy-based sizing procedure is formulated in this study for this class of dampers, where the total number of constituting plates is directly related, without iterative steps, to the supplementary damping energy required to jointly reduce stress states in structural members and storey drifts. The stiffening effects of the dissipative braces are expressly controlled, so as to compensate for the increase in storey shears induced by their incorporation in the frame skeleton. The sizing procedure is demonstratively applied to the retrofit design of a 6-storey reinforced concrete building, to explicate and discuss the use of its analytical relations and relevant limitations in practice. The evaluation of the seismic performance of the structure in retrofitted conditions allows comparing the response of the dissipative braces.

KEYWORDS

added stiffness, added damping, dampers, design, sizing, seismic retrofit, frame structures

1 Introduction

Seismic retrofit strategies of frame structures are quickly evolving, and several significant contributions have been recently offered in terms of design approaches and modelling (Marano et al., 2007; Greco and Marano, 2016; Di Trapani et al., 2020; Aloisio et al., 2022), as well as of implementation of innovative protection techniques or upgrade of existing ones (Aloisio et al., 2022; Boggian et al., 2022; Lu and Phillips, 2022; Zhao et al., 2022).

Among the strategies based on the incorporation of supplementary damping devices, those making use of Added Damping and Stiffness (ADAS) steel dissipators have a well-established tradition (Bergman and Goel, 1987; Whittaker et al., 1991; Aiken et al., 1993; Martinez-Romero, 1993; Tsai et al., 1993; Dargush and Soong, 1995), updated to recent developments too (Mazza, 2014; Teruna, 2015; Moghaddasi and Namazi, 2016; Sorace et al., 2016; Mohammadi et al., 2017; Mazza and Imbrogno, 2019; Shojaeifar et al., 2020; Gandelli et al., 2021; Khoshkalam et al., 2022). This is a consequence of the plain working principle of these devices, based on the elastic-plastic behaviour of the constituting plates, as well as of their relatively easy installation. In spite of this, the design of ADAS dampers is not an easy task, as it requires a proper balance between the addition of energy dissipation and horizontal translational stiffness. The former allows remarkably reducing plastic demand on structural members. The latter is always beneficial in terms of lateral displacements but, as long as the dampers respond elastically, can cause a significant increase in base and storey shears, and thus in the stress states of the frame skeleton elements and foundations.

In view of this, an energy-based preliminary sizing criterion of ADAS dampers was proposed by the first two authors of this article (Sorace et al., 2016), aimed at achieving a joint control of stress states and displacements. According to this criterion, typically framed within a performance-based design approach (SEAOC, 1995; Priestley, 1997; Priestley and



Calvi, 1997; Fardis. 2007; Priestley et al., 2007), the total number of plates is tentatively fixed by: 1) pre-estimating the energy dissipation capable of providing a target drop of base shear in retrofitted conditions; 2) computing the energy dissipation capacity by assuming a maximum displacement of the dissipators calibrated on a target reduction of storey drifts. By expanding and developing this method, a new sizing procedure is formulated in this article, where the energy dissipation capacity of the dampers is evaluated by expressly compensating the bracing-related increase of base shear, caused by the increase in lateral stiffness of the structure.

The distinguishing features of the procedure, as compared to other existing methods, can be synthesized in the two following points: 1) it provides a quick estimate of the energy demand on the protective system, based on simple analytical relations making use of spectral displacement, velocity, and pseudo-acceleration ordinates; 2) it is intrinsically not iterative, as these relations are linear.

Concerning the application of the procedure, the use of spectral quantities produces the best approximation for structures characterized by first translational modes along the two coordinate axes in plan with associated modal masses constituting a predominant portion of the total seismic masses. This condition is basically met by structures with a rather regular geometry in plan and elevation. However, in order to effectively apply the sizing procedure to irregular structures too, a modulating coefficient of the energy dissipation demand is included to compensate for higher translational modes and/or plan torsion response effects.

The formulation of the sizing criterion is presented in Section 2. A demonstrative application is offered in Section 3, Section 4, concerning the retrofit design of a representative case study, i.e., a 6-storey residential building with reinforced concrete (RC) structure situated in L'Aquila, Abruzzo, Italy. Based on the results of a seismic assessment analysis initially carried out on the building (Section 3), the application of the procedure is explicated and discussed in detail in Section 4.1, Section 4.2. The performance of the structure in retrofitted conditions is finally evaluated (Section 4.3), to compare the response of the designed ADAS-equipped dissipative bracing system with the hypotheses formulated at the sizing stage.

2 Design criterion for ADAS dissipators

ADAS dissipators consist of an assembly of multiple X-shaped or isosceles triangle-shaped (in which case they are named T-ADAS) steel plates mounted in parallel, which act as short cantilever beams with cross section linearly varying along the span, similarly to the bending moment diagram.

Figure 1 shows the drawing of a T-ADAS damper, the geometry of a constituting plate and the P(t)-d(t) force–displacement hysteretic response cycle of the latter, idealized with a bilinear hardening shape. The mechanical parameters governing the cycle are: P_{y} , P_u = yielding and ultimate force, d_y , d_u = yielding and ultimate displacement, all intended with positive and negative sign, k_e , k_p = stiffness of the elastic and post-elastic response branch, and $\gamma = k_p/k_e$ = strain hardening ratio of the post-elastic branch, normally assumed as equal to 0.03 (Dargush and Soong, 1995).

Based on the geometric symbols in Figure 1, and named f_y the yielding stress of steel, the expressions of the response cycle parameters are as follows:

$$P_y = f_y \frac{BT^2}{6H} \tag{1}$$

$$d_y = \frac{P_y}{k_z} \tag{2}$$

$$k_e = E_s \frac{BT^3}{6H^3} \tag{3}$$

$$k_p = \gamma k_e \tag{4}$$

$$P_u = f_y \frac{BT^2}{4H} \tag{5}$$

$$d_u = d_y + \frac{P_u - P_y}{k_p} \tag{6}$$

The preliminary sizing procedure of the dampers proposed in this study is aimed at evaluating the number of plates to be installed in the bracing system, n_{pb} starting from a quick estimation of the energy dissipation capacity by which a pre-established reduction of lateral displacements and base shear of the structure is attained. For frame buildings with a substantially regular geometry in plan and elevation, this estimation is carried out in terms of spectral quantities, by referring to the periods of the first translational modes along the two coordinate axes in plan (which a predominant portion of modal masses is associated with, in the above-mentioned hypothesis of approximate regularity). Both in current and retrofitted conditions, these periods are assumed to be included in the wide period interval of the normative response spectra that corresponds to the constant pseudo-velocity branch, identified by the periods limits T_c and T_D , where the fundamental vibration



periods of low rise through mid-to-high rise RC frame structures are situated.

For both axes in plan, X and Y, of the reference Cartesian coordinate system assumed in the analysis, named T_{IN} the fundamental period of the structure in current state, the procedure starts by fixing a tentative reduction, ΔS_{D} , in the spectral displacement computed for T_{IN} . Consistently with the first mode-based quick estimation of seismic response adopted here, the difference between S_D (T_{IN}) and ΔS_D is put as equal to an assumed target value of the top lateral displacement of the structure, $D_{top.tarv}$:

$$S_D(T_{IN}) - \Delta S_{D-} = D_{top,targ} \tag{7}$$

from which ΔS_{D-} derives:

$$\Delta S_{D-} = S_D(T_{IN}) - D_{top,targ} \tag{8}$$

Then, named $S_{V,cost}$ the value of the horizontal branch of the pseudo-velocity spectrum, the period in retrofitted conditions, T_{FIN} , given by the difference between T_{IN} and the period reduction ΔT corresponding to ΔS_{D-} , can be evaluated as follows:

$$T_{FIN} = T_{IN} - \Delta T = T_{IN} - \frac{2\pi\Delta S_{D-}}{S_{V,cost}}$$
(9)

As illustrated in Figure 2, a ΔS_{A+} rise in pseudo-acceleration is generated when passing from T_{IN} to T_{FIN} , as a consequence of the increase in lateral stiffness induced by the incorporation of the dissipative bracing system. Therefore, its supplementary damping contribution must contextually generate a drop in the spectral ordinate, $\Delta S_{A-,diss}$, so as to decrease base shear—or, when deemed sufficient, to limit its growth—as compared to current conditions. Consistently, $\Delta S_{A-,diss}$ is tentatively fixed in proportion to ΔS_{A+} , by means of an energy dissipation demand coefficient, m_{ed} , to be calibrated on the design objective(s) fixed in terms of base shear. This condition is expressed as:

$$\Delta S_{A-,diss} = m_{ed} \Delta S_{A+} \tag{10}$$

where $m_{ed} > 1$ targets to reduce both lateral displacements and base shear, whereas $m_{ed} \le 1$ only the former. It can be noted that a moderate increase in base shear can be often accepted, since a significant portion of storey shears is absorbed, as axial forces, by the diagonal trusses of the bracing system. This allows remarkably reducing bending

moments and shears in beams and columns, as targeted in the design, only causing an increase of axial forces in the columns belonging to the vertical alignments where the system is placed, as well as of the stress states in the underlying portions of the foundations. Therefore, in order to prevent an excessive addition of supplementary damping, m_{ed} values equal to or slightly greater than 1 (i.e., equal to 1.1-1.2), and in some cases even slightly smaller than 1, can be adopted, especially for regular structures. At the same time, greater m_{ed} values are normally needed for irregular structures, to compensate for possible significant contributions of the higher translational modes, and/or plan torsion response effects related to the rotational modes around the vertical axis of the reference coordinate system. Furthermore, m_{ed} values greater than 1 are normally needed for frame structures, with RC or steel skeleton, characterized by rather high fundamental vibration periods (e.g., greater than 1.5 s), since in these cases a greater increase in lateral stiffness-and thus in base shear-is induced by the stiffening action of the bracing system.

The supplementary damping-related reduction in base shear, ΔV , is obtained by multiplying $\Delta S_{A,diss}$ by the seismic mass M of the building. Hence, the tentative energy dissipation capacity to be assigned to the protective system is computed as:

$$E_d = 4\Delta V \Delta S_{D-} = 4M\Delta S_{A-,diss} \Delta S_{D-} = 4Mm_{ed} \Delta S_{A+} \Delta S_{D-}$$
(11)

By separately applying relations (Eq. 7) through (Eq. 11) for the X and Y axes, the corresponding energy dissipation capacities, $E_{d,X}$, $E_{d,Y}$, are obtained. Then, the total numbers of plates of the sets of ADAS dampers to be installed in X and Y, $n_{p,X}$, $n_{p,Y}$, are evaluated by dividing $E_{d,X}$, $E_{d,Y}$ by the estimated total energy dissipated by each plate, $E_{d,p,t}$ under the input ground motions assumed in the design analyses. $E_{d,p,t}$ is calculated by computing, at a first step, the $E_{d,p,c}$ energy dissipated by a plate in a cycle bounded by the maximum estimated (positive or negative) displacement, $d_{max,e}$ (symbolically indicated in the graph of Figure 1 too), given by:

$$E_{d,p,c} = 2P_y \cdot 2(d_{max,e} - d_y) \tag{12}$$

Then, $E_{d,p,t}$ is obtained by summing to $E_{d,p,c}$ the energy dissipated in all remaining cycles with smaller amplitudes, $E_{d,p,r}$. $E_{d,p,r}$ was evaluated to be about 10 times greater than $E_{d,p,c}$ in a recent extensive numerical research (Gandelli et al., 2021). At the same time, a similar value was preliminarily estimated in this study for simpler frame structures than the case study one, not reported here for brevity's sake, by extending the findings of a previous study of the authors carried out for a special infrastructure (Sorace et al., 2016). Based on this approximate $E_{d,p,r}$ value, the tentative evaluation of $E_{d,p,t}$ results as follows:

$$E_{d,p,t} = E_{d,p,c} + E_{d,p,r} = (1+10)E_{d,p,c} = 11E_{d,p,c}$$
(13)

Thus, $n_{p,X}$, $n_{p,Y}$ are finally evaluated as follows:

$$n_{p,X} = \frac{E_{d,X}}{E_{d,p,t}} \tag{14a}$$

$$n_{p,Y} = \frac{E_{d,Y}}{E_{d,p,t}} \tag{14b}$$

For the practical application of Eqs 12, 13, $d_{max,e}$ must be preliminarily quantified. This can be done by relating it to the maximum inter-storey drift (ID_m) of the structure, and fixing a target design value for the latter, $ID_{m,t}$. By considering that the



supporting diagonal braces of the ADAS devices are remarkably rigid at the horizontal translation, and thus lateral displacements are mainly determined by the plastic deformation of the dissipators (Sorace et al., 2016), at the sizing stage $d_{max,e}$ can be approximately assumed to coincide with $ID_{m,t}$.

The latter is calibrated on the specific characteristics of each case study and the severity of the basic earthquake level considered in the performance assessment analysis (formally defined in the next section). By way of example, in order to limit damage to a fully repairable level in masonry infill and partition panels of RC frame buildings, when they are built in contact with the structural members, named *IH* the inter-storey height, $ID_{m,t}$ could be tentatively put as equal to 0.5% of IH, i.e., the limit fixed by the Italian Technical Standards (Italian Ministry of Infrastructure and Transport, 2018) as basic requirement for the attainment of the Immediate Occupancy (IO) performance level. The same drift limitation is assumed by internationally prominent performance-based seismic Standards and Guidelines, among which SEAOC Vision 2000 (SEAOC, 1995), FEMA 356 (ASCE, 2000), ATC 58-2 (ATC, 2003), ASCE/SEI 41 (ASCE, 2017), as repairability threshold for unreinforced masonry infill and partition walls.

3 Case study building

The examined case study is a residential building, located in L'Aquila, Abruzzo, Italy, designed in compliance with the 1986 edition of the Italian Seismic Standards, where a maximum pseudo-acceleration spectral ordinate of 0.07 g (g = acceleration of gravity) was prescribed for the corresponding seismic zone. As illustrated in Figure 3, referred to the ground storey, the building has a 21.05 × 11.45 m² sized rectangular plan, with the first side parallel to the *X* axis and the second one to the *Y* axis of the assumed Cartesian reference system. The building has six above-ground storeys in elevation, with inter-storey heights equal to 3.4 m for the ground storey and 3.04 m for the remaining ones.

The structure is constituted by a RC frame skeleton. Columns are of five types, named CT1 through CT5, having the following cross sections and steel reinforcing bars: $CT1-300 \times 600$ (side parallel to X×side parallel to Y) mm², 8 \emptyset 14; CT2 $-300 \times 550 \text{ mm}^2$, 8 \emptyset 14; CT3 $-500 \times 300 \text{ mm}^2$, 6ø14; CT4 $-300 \times 400 \text{ mm}^2$, 4ø14; and CT5 $-300 \times 300 \text{ mm}^2$, 4ø12. The transversal reinforcement is constituted by 200 mm-spaced ø6 stirrups for all columns. By way of example, the column types-vertical fixed lines association on the ground storey is the following (Figure 3): CT1-2/B, 5/B, 2/C, 3/C, 4/ C, 5/C (columns with acronym printed in red); CT2—3/B, 4/B, 3/D, 4/ D (grey); CT3-2/A, 3/A, 4/A, 5/A, 2/D, 5/D (green); CT4-1/A, 6/A, 1/B, 6/B, 1/C, 6/C, 1/D, 6/D (black). The cross sections of columns CT1 through CT4 are also drawn in Figure 3. The association for the entire structure is recapitulated in Table 1. On all storeys, perimeter beams (named BT1 in Figure 3) have out-of-depth section sized $300 \times$ 500 (base×height) mm², with constant reinforcement given by 3ø16 top bars and 2ø16 bottom bars, and 200 mm-spaced ø6 stirrups; internal beams parallel to X (BT2) have in-depth sections sized $600 \times 250 \text{ mm}^2$, with a maximum of 8ø16 top bars and 6ø16 bottom bars, and ø6 stirrups with spacing varying from

TABLE 1 Column sections.

Storey	Column type	Vertical fixed lines						
G	CT1	2/B, 5/B, 2/C, 3/C, 4/C, 5/C						
	CT2	3/B, 4/B						
	CT3	2/A, 3/A, 4/A, 5/A, 2/D, 3/D, 4/D, 5/D						
	CT4	1/A, 6/A, 1/B, 6/B, 1/C, 6/C, 1/D, 6/D						
	CT5	_						
1	CT1	_						
	CT2	_						
	CT3	2/C, 3/C, 4/C, 5/C						
	CT4	2/A, 3/A, 4/A, 5/A, 2/B, 3/B, 4/B, 5/B, 2/D, 3/D, 4/D, 5/D						
	CT5	1/A, 6/A, 1/B, 6/B, 1/C, 6/C, 1/D, 6/D						
2	CT1	_						
	CT2	_						
	CT3	_						
	CT4	2/B, 5/B, 2/C, 3/C, 4/C, 5/C						
	CT5	1/A, 2/A, 3/A, 4/A, 5/A, 6/A, 1/B, 3/B, 4/B, 6/B, 1/C, 6/C, 1/D, 2/D, 3/D, 4/D, 5/D, 6/D						
3	CT1	_						
	CT2	_						
	CT3	_						
	CT4	_						
	CT5	1/A, 2/A, 3/A, 4/A, 5/A, 6/A, 1/B, 2/B, 3/B, 4/B, 5/B, 6/B, 1/C, 2/C, 3/C, 4/C, 5/C, 6/C, 1/D, 2/D, 3/D, 4/D, 5/D, 6/D						
4	CT1	_						
	CT2	_						
	CT3	_						
	CT4	_						
	CT5	1/A, 2/A, 3/A, 4/A, 5/A, 6/A, 1/B, 2/B, 3/B, 4/B, 5/B, 6/B, 1/C, 2/C, 3/C, 4/C, 5/C, 6/C, 1/D, 2/D, 3/D, 4/D, 5/D, 6/D						
5	CT1	_						
	CT2	_						
	CT3	_						
	CT4	_						
	CT5	1/A, 2/A, 3/A, 4/A, 5/A, 6/A, 1/B, 2/B, 3/B, 4/B, 5/B, 6/B, 1/C, 2/C, 3/C, 4/C, 5/C, 6/C, 1/D, 2/D, 3/D, 4/D, 5/D, 6/D						

70 mm to 200 mm; internal beams parallel to *Y* (BT3) have in-depth sections sized 800 × 250 mm², with a maximum of 8ø20 top bars and 5ø20 bottom bars, and ø6 stirrups with spacing varying from 150 mm to 200 mm. The flights of stairs, embedded in the 3/C-3/D and 4/C-4/D alignments in plan, are borne by inclined beams (BT4) having 300 × 400 mm² section, with constant 4ø14 top and 4ø14 bottom bars, and 200 mm-spaced ø6 stirrups. The foundations are constituted by a mesh of inverse T-shaped RC beams. Their base sections are 2,600 mm-wide in *Y* direction and 1,600 mm-wide in *X*, with 1,200 mm (*Y*) and 800 (*X*) mm-high webs, and 600 mm (*Y*) and 400 mm (*X*) mm-high RC joists, parallel to *X* axis, interposed clay lug

bricks, and a 50 mm thick upper RC slab. Both for the elevation and foundation structures, reinforcing bars are made of FeB44k steel, with yield stress and tensile strength values greater than 430 MPa and 540 MPa, respectively; and concrete is 25/30 class, with cylindrical and cubic compressive strength of 25 MPa and 30 MPa, respectively. The dead and live loads assumed in the analyses are as follows: 5 kN/m^2 (dead) and 2 kN/m^2 (live) on first through fifth floor; 3.8 kN/m^2 and 1.2 kN/m^2 on sixth (roof) floor. The live loads on the stairwell are equal to 4 kN/m^2 .

A view of the finite element model of the structure, generated by SAP2000NL software (CSI, 2022), is displayed in Figure 4, where the Cartesian reference system is traced out too. Elastic frame elements





were used to model columns and beams, consistently with the choice of evaluating the effectiveness of the sizing procedure within a conventional elastic analysis approach, where seismic performance in retrofitted conditions is assessed in terms of reductions of stress states in structural members and inter-storey drifts, as compared to current state. A Rayleigh-type inherent viscous damping was assigned to the finite element structural model.

A modal analysis carried out by this model highlighted two main translational modes in current state, whose shapes are plotted in Figure 4 too, with vibration period, T_{IN} , equal to 1.21 s along X and 1.18 s along Y, and effective modal masses of 86.4% and 85.7%, respectively, of the total seismic mass M of the building, equal to 1,675 kN/g. Both values are greater than the 85% threshold representing the minimum percentile fraction required by the Italian Technical Standards to develop a modal superposition analysis. Period and effective mass of the first rotational mode around the vertical axis Z are equal to 1.05 s and 81.1%, respectively. As a consequence of the substantial structural regularity in plan and elevation, a total of nine modes is needed to activate summed modal masses greater than 90% of M along X, Y, and around Z, and a total of eighteen modes to attain over than 99% of M.

The seismic assessment study of the building was developed *via* time-history analysis by using as input a set of seven groups of three

accelerograms. For each group, one accelerogram was applied in X direction, one in Y, and one in Z. The artificial ground motions were generated from the elastic pseudo-acceleration response spectra at linear viscous damping ratio of 0.05 assumed by the current Italian Technical Standards for L'Aquila, drawn in Figure 5. The three spectral graphs for the horizontal components and the three graphs for the vertical one are referred to the Serviceability Design Earthquake (SDE, characterized by 63% probability of being exceeded over the reference structural lifespan, V_R), Basic Design Earthquake (BDE, with $10\%/V_R$ probability) and Maximum Considered Earthquake (MCE, with 5%/V_R probability) hazard levels, for C-type (i.e., medium-dense sand) soil and T1-type (i.e., flat surface) topographic category. The corresponding peak ground acceleration values are: 0.156 g (SDE), 0.347 g (BDE), and 0.407 g (MCE), for the horizontal components; 0.045 g (SDE), 0.180 g (BDE), and 0.261 g (MCE), for the vertical one.

The results of the analysis in current conditions are synthesized in the top halves of Tables 2, 3. Table 2 reports the maximum storey shears along the two axes in plan, $V_{m,X}$ and $V_{m,Y}$, and their ratios, $\rho_{V,X}$ and $\rho_{V,Y}$, to relevant strength values, $V_{R,X}$ and $V_{R,Y}$ (where $V_{R,X}$, $V_{R,Y}$ are given by the sums of the shear strength values of the ground storey columns). Table 3 lists the maximum inter-storey drifts, $ID_{m,X}$, $ID_{m,Y}$, and their ratios, $\rho_{ID,X}$ and $\rho_{ID,Y}$, to *IH*.

Current conditions																							
S				SDE			BC	DE		MCE													
	V _{R,X} (kN)	V _{R,Y} (kN)	<i>V_{m,X}</i> (kN)	<i>V_{m,Y}</i> (kN)	ρ _{v,x}	ρ _{v,y}	<i>V_{m,X}</i> (kN)	<i>V_{m,Y}</i> (kN)	ρ _{ν,χ}	ρ _{v,y}	V _{m,X} (kN)	<i>V_{m,Y}</i> (kN)	ρ _{v,x}	$ ho_{V,Y}$									
1	1996	2337	2372	2711	1.19	1.16	5967	6193	2.99	2.65	7315	7890	3.66	3.38									
2	1814	1912	1846	1950	1.02	1.02	4245	4354	2.34	2.28	5259	5403	2.89	2.83									
3	1747	1813	1554	1579	0.89	0.87	3301	3388	1.89	1.87	4123	4257	2.36	2.34									
4	1696	1696	1129	1157	0.67	0.68	2419	2531	1.43	1.49	3002	3093	1.77	1.82									
5	1696	1696	802	827	0.47	0.48	1713	1745	1.01	1.03	2103	2074	1.21	1.24									
6	1696	1696	374	378	0.22	0.22	984	1018	0.58	0.60	890	975	0.52	0.57									
				1	1							Retrofitted Conditions											
						Retrof	fitted Condition	S					1										
S				SDE		Retrof	fitted Condition BI	s DE				MCE											
S	V _{R,X} (kN)	V _{R,Y} (kN)	V _{m,X} (kN)	SDE V _{m,Y} (kN)	$ ho_{V,X}$	Retrof Pv,y	fitted Condition BI <i>V_{m,X}</i> (kN)	s DE <i>V_{m,Y}</i> (kN)	ρν,χ	ρ _{ν,γ}	V _{m,X} (kN)	MCE <i>V_{m,Y}</i> (kN)	ρν,χ	<i>ρ</i> ν,γ									
S	V _{R,X} (kN) 1996	V _{R,Y} (kN) 2337	V _{m,X} (kN) 1956	SDE <i>V_{m,Y}</i> (kN) 2430	ρ _{V,X} 0.98	Retrof <i>ρ_{V,Y}</i> 1.04	fitted Condition Bl V _{m,X} (kN) 4970	s DE <i>V_{m,Y}</i> (kN) 5304	ρ _{V,X} 2.49	ρ _{V,Y} 2.27	V _{m,X} (kN) 5037	МСЕ <i>V_{m,Y}</i> (kN) 6240	ρ _{V,X} 2.97	<i>Ρ</i> ν,γ 2.67									
S 1 2	V _{R,X} (kN) 1996 1814	V _{R,Y} (kN) 2337 1912	V _{m,X} (kN) 1956 1505	SDE <i>V_{m,Y}</i> (kN) 2430 1683	<i>ρ</i> _{V,X} 0.98 0.83	Retrof <i>Ρν,γ</i> 1.04 0.88	fitted Condition BI <i>V_{m,X}</i> (kN) 4970 3320	s DE <i>V_{m,Y}</i> (kN) 5304 3614	<i>ρν,χ</i> 2.49 1.83	<i>Ρν,γ</i> 2.27 1.89	V _{m,X} (kN) 5037 4100	MCE <i>V_{m,Y}</i> (kN) 6240 4512	ρ _{V,X} 2.97 2.26	<i>ρ</i> ν,γ 2.67 2.36									
S 1 2 3	V _{R,X} (kN) 1996 1814 1747	V _{R,Y} (kN) 2337 1912 1813	V _{m,X} (kN) 1956 1505 1380	SDE V _{m,Y} (kN) 2430 1683 1504	<i>P</i> _{V,X} 0.98 0.83 0.79	Retrof <i>Pv,y</i> 1.04 0.88 0.83	fitted Condition Bl <i>V_{m,X}</i> (kN) 4970 3320 2568	s DE <i>V_{m,Y}</i> (kN) 5304 3614 2774	<i>ρν,χ</i> 2.49 1.83 1.47	<i>Ρν,γ</i> 2.27 1.89 1.53	V _{m,X} (kN) 5037 4100 3162	MCE <i>V_{m,Y}</i> (kN) 6240 4512 3427	<i>Ρν.x</i> 2.97 2.26 1.81	<i>ρν,γ</i> 2.67 2.36 1.89									
S 1 2 3 4	V _{R,X} (kN) 1996 1814 1747 1696	V _{R,Y} (kN) 2337 1912 1813 1696	V _{m,X} (kN) 1956 1505 1380 1068	SDE <i>V_{m,Y}</i> (kN) 2430 1683 1504 1085	<i>ρ</i> _{V,X} 0.98 0.83 0.79 0.63	Retrof <i>Pv,γ</i> 1.04 0.88 0.83 0.64	fitted Condition Bl <i>V_{m,X}</i> (kN) 4970 3320 2568 1967	s DE <i>V_{m,Y}</i> (kN) 5304 3614 2774 2188	<i>ρ_{V,X}</i> 2.49 1.83 1.47 1.16	<i>ρ_{V,Y}</i> 2.27 1.89 1.53 1.29	V _{m,X} (kN) 5037 4100 3162 2544	MCE <i>V_{m,Y}</i> (kN) 6240 4512 3427 2222	<i>ρν,χ</i> 2.97 2.26 1.81 1.39	<i>Ρν,γ</i> 2.67 2.36 1.89 1.50									
S 1 2 3 4 5	<i>V_{R,X}</i> (kN) 1996 1814 1747 1696 1696	V _{R,Y} (kN) 2337 1912 1813 1696 1696	V _{m,X} (kN) 1956 1505 1380 1068 729	SDE <i>V_{m,Y}</i> (kN) 2430 1683 1504 1085 763	<i>ρ</i> _{V,X} 0.98 0.83 0.79 0.63 0.43	Retrof <i>Pv,γ</i> 1.04 0.88 0.83 0.64 0.45	fitted Condition Bl V _{m,X} (kN) 4970 3320 2568 1967 1322	s DE <i>V_{m,Y}</i> (kN) 5304 3614 2774 2188 1459	<i>ρν,χ</i> 2.49 1.83 1.47 1.16 0.78	<i>Ρν,γ</i> 2.27 1.89 1.53 1.29 0.86	V _{m,X} (kN) 5037 4100 3162 2544 1662	MCE <i>V_{m,Y}</i> (kN) 6240 4512 3427 2222 1509	<i>ρν.x</i> 2.97 2.26 1.81 1.39 0.92	<i>ρν</i> , <i>γ</i> 2.67 2.36 1.89 1.50 0.98									

TABLE 2 V_{m,X}, V_{m,Y} maximum storey shears, and corresponding $\rho_{V,X}$, $\rho_{V,Y}$ ratios to relevant V_{R,X}, V_{R,Y} strength values, in current and retrofitted conditions.

Current conditions														
S		SDE					BDE			MCE				
	IH (m)	<i>ID_{m,X}</i> (mm)	<i>ID_{m,Y}</i> (mm)	ρ _{ID,X} (%)	ρ _{ID,Y} (%)	<i>ID_{m,X}</i> (mm)	<i>ID_{m,Y}</i> (mm)	ρ _{ID,X} (%)	ρ _{ID,Y} (%)	<i>ID_{m,X}</i> (mm)	<i>ID_{m,Y}</i> (mm)	ρ _{ID,X} (%)	ρ _{ID,Y} (%)	
G	3.40	15.1	13.6	0.44	0.40	31.7	29.2	0.93	0.86	38.8	35.9	1.14	1.06	
1	3.04	16.2	14.7	0.53	0.48	39.8	37.7	1.24	1.15	45.9	43.2	1.51	1.42	
2	3.04	15.5	13.7	0.51	0.45	37.5	36.4	1.17	1.11	42.3	40.4	1.39	1.33	
3	3.04	13.2	11.6	0.43	0.38	29.6	28.9	0.94	0.91	35.9	34.5	1.18	1.13	
4	3.04	10.7	9.9	0.35	0.33	20.5	20.3	0.67	0.67	25.8	25,1	0.85	0.83	
5	3.04	7.4	6.9	0.24	0.23	11.9	11.7	0.39	0.38	13.9	13.1	0.46	0.43	
	Retrofitted Conditions													
S			SDE			BDE				MCE				
	<i>IH</i> (m)	<i>ID_{m,X}</i> (mm)	<i>ID_{m,Y}</i> (mm)	$ ho_{ID,X}$ (%)	ρ _{ID,Y} (%)	<i>ID_{m,X}</i> (mm)	<i>ID_{m,Y}</i> (mm)	ρ _{ID,X} (%)	ρ _{ID,Y} (%)	<i>ID_{m,X}</i> (mm)	<i>ID_{m,Y}</i> (mm)	ρ _{ID,X} (%)	ρ _{ID,Y} (%)	
G	3.40	7.3	7.6	0.21	0.22	14.3	14.9	0.42	0.44	16.9	17.3	0.50	0.51	
1	3.04	7.9	8.3	0.26	0.27	15.6	15.9	0.51	0.52	19.6	20.2	0.64	0.66	
2	3.04	7.2	7.5	0.24	0.25	14.8	15.2	0.49	0.50	18.3	19.4	0.60	0.64	
3	3.04	4.7	5.1	0.15	0.17	12.6	13.0	0.41	0.43	15.9	16.8	0.52	0.55	
4	3.04	3.2	3.6	0.11	0.12	9.3	9.7	0.31	0.32	11.8	12,7	0.39	0.42	

3.9

0.12

0.13

5.6

3.6

TABLE 3 ID_{m,Xr} ID_{m,Y} maximum inter-storey drifts, and corresponding $\rho_{id,Xr}$ $\rho_{id,Xr}$ ratios to relevant IH inter-storey heights, in current and retrofitted conditions.

5

3.04

1.2

1.4

0.04

0.05

6.4

0.18

0.21



 M_1-M_2 biaxial moment interaction curves (red lines) for the columns belonging to the 3/B vertical fixed line obtained from the most demanding BDE scaled group of input accelerograms, and relevant safe domains (blue lines).

As shown in Table 2, $\rho_{s,X}$, $\rho_{s,Y}$ ratios greater than 1 are found for the first two, four and five storeys at the SDE, BDE, and MCE, respectively, reaching values of 1.19, 2.99, 3.66 ($\rho_{s,X}$), and 1.16, 2.65, 3.38 ($\rho_{s,Y}$) on the ground storey. Values notably below 1 come out for the top storey up to the MCE. The corresponding results in terms of stress states in the structural members highlight 22%, 72%, and 81% of columns, and 18%, 68%, and 76% of beams in unsafe conditions at the SDE, BDE, and MCE, respectively. By way of example of these results, the M_1 - M_2 biaxial moment interaction curves obtained at the BDE for the columns belonging to the 2/B vertical fixed line—where M_1 , M_2 are the bending moments around the two local reference axes of the column cross section-are plotted in Figure 6. Except for the top storey, these curves remarkably overcome the boundaries of the axial force-biaxial moment safe domains, traced out for comparison in the same graphs, reaching maximum values of the demand/capacity ratio equal to 2.23 (ground storey), 1.76 (first), 1.98 (second), 1.84 (third), and 1.65 (fourth).

Table 3 highlights that the $\rho_{ID,X}$ ratios at the SDE are slightly greater than the above-mentioned IO performance level-related 0.5% *IH* limit ($\rho_{ID,X}$ = 0.53%, 0.51% on the first and second storey,

respectively), assessing a satisfactory performance in terms of drifts for this earthquake level. At the same time, $\rho_{ID,X}$ and $\rho_{ID,Y}$ ratios slightly smaller than 1 are observed at the BDE on the ground and third storey, and greater than 1 on the first and second storey, reaching $\rho_{ID,X}$ peak values of 1.24% (first) and 1.17% (second), and $\rho_{ID,Y}$ peak values of 1.15% (first) and 1.11% (second), implicitly assessing irreparable damage conditions of infills and partitions at these storeys. At the MCE, $\rho_{ID,X}$ and $\rho_{ID,Y}$ values greater than 1 are observed on the four lower storeys, with maximum values of 1.51 ($\rho_{ID,X}$) and 1.42 ($\rho_{ID,Y}$) on the first storey.

4 Retrofit intervention

4.1 Pre-sizing of dampers

By referring to the nomenclature in Figure 1, the retrofit intervention on the case study building was designed by assuming the following classical (Martinez-Romero, 1993; Tsai et al., 1993; Dargush and Soong 1995) geometric sizes of the plates: H = 150 mm, t = 15 mm, and B = 75 mm. The constituting steel is type





S275, with yield stress and tensile strength equal to 275 N/mm² and 430 N/mm², respectively. For these geometrical and mechanical characteristics, the following values of the yielding force and

displacement of a plate, to be introduced in relation (12), are obtained by means of expressions 1) and 2): $P_y = 5.156$ kN, $d_y = 1.96$ mm.





 M_1-M_2 biaxial moment interaction curves (red lines) for the columns belonging to the 3/B vertical fixed line obtained from the most demanding BDEscaled group of input accelerograms in retrofitted conditions, and relevant safe domains (blue lines).

According to the approach followed in recent multi-objective sizing procedures of dampers for the seismic retrofit of frame buildings (Lavan and Dargush, 2009; Akehashi and Takewaki, 2021; De Domenico and Hajirasouliha, 2021), the design of the protective system is carried out for the BDE hazard level, with checks extended to the SDE and the MCE in the final verification



analysis. In order to apply the sizing criterion presented in Section 2, the $d_{max,e}$ maximum plate displacement, to be introduced in Eq. 12 too, is put as equal to $ID_{m,t} = 0.5\%$ *IH*, by referring to the greater interstorey height, equal to 3.4 m. Thus, the following value results: $d_{max,e} = (0.005 \cdot 3,400)$ mm = 17 mm. Consistently with this assumption, $D_{top,targ}$ is put as equal to 0.5% of the total height of the structure (18.6 m), which yields: $D_{top,targ} = (0.005 \cdot 18,600)$ mm = 93 mm, both in *X* and *Y*. Moreover, by considering the substantial regularity of the case study structure, $m_{ed} = 1$ is tentatively considered in (10).

Based on these hypotheses, the application of the criterion is separately detailed below for the two axes (thus, lower indexes X, Y are added to all quantities and symbols introduced in the previous sections).

4.1.1 X direction

$$\begin{split} T_{IN,X} &= 1.21 \text{ s} \\ S_{D,X}(T_{IN,X}) &= 159.4 \text{ mm} \\ S_{A,X}(T_{IN,X}) &= 0.349 \text{ g} \\ S_{V,cost} &= 665.7 \text{ mm/s} \\ D_{top,targ} &= 93 \text{ mm} \\ \Delta S_{D-,X} &= S_{D,X}(T_{IN,X}) - D_{top,targ} = 66.4 \text{ mm} \\ \text{By (9): } T_{FIN,X} &= 0.584 \text{ s} \\ S_{A,X}(T_{FIN,X}) &= 0.723 \text{ g} \end{split}$$

$$\begin{split} &\Delta S_{A+,X} = S_{A,X}(T_{FIN,X}) - S_{A,X}(T_{IN,X}) = 0.374 \text{ g} \\ &\text{By (10), for } m_{ed} = 1: \Delta S_{A-,diss,X} = \Delta S_{A+,X} = 0.374 \text{ g} \\ &\text{By (11), for } M = 1675 \text{ kN/g}: E_{d,X} = (4 \cdot 1675 \cdot 9.81 \cdot 0.374 \cdot 0.0664) \\ &\text{kJ} = 1632 \text{ kJ} \\ &\text{By (12), for } d_{max,e} = 17 \text{ mm}: E_{d,p,c,X} = [2 \cdot 5.156 \cdot 2 \cdot (17 - 1.96)] \text{ J} = \\ &310 \text{ J} = 0.31 \text{ kJ} \\ &\text{By (13): } E_{d,p,t,X} = (11 \cdot 0.31) \text{ kJ} = 3.41 \text{ kJ} \\ &\text{By (14a): } n_{p,X} = E_{d,X}/E_{d,p,t,X} = 479 \end{split}$$

4.1.2 Y direction

$$\begin{split} T_{IN,Y} &= 1.18 \text{ s} \\ S_{D,Y}(T_{IN,Y}) &= 155.4 \text{ mm} \\ S_{A,Y}(T_{IN,Y}) &= 0.358 \text{ g} \\ S_{V,cost} &= 665.7 \text{ mm/s} \\ D_{top,targ} &= 93 \text{ mm} \\ \Delta S_{D_{-}Y} &= S_{D,Y}(T_{IN,Y}) - D_{top,targ} = 62.4 \text{ mm} \\ \text{By (9): } T_{FIN,Y} &= 0.591 \text{ s} \\ S_{A,Y}(T_{FIN,Y}) &= 0.719 \text{ g} \\ \Delta S_{A+,Y} &= S_{A,Y}(T_{FIN,Y}) - S_{A,Y}(T_{IN,Y}) = 0.361 \text{ g} \\ \text{By (10), for } m_{ed} &= 1: \Delta S_{A-,diss,Y} = \Delta S_{A+,Y} = 0.361 \text{ g} \\ \text{By (11), for } M &= 1675 \text{ kN/g: } E_{d,Y} = (4 \cdot 1675 \cdot 9.81 \cdot 0.361 \cdot 0.0624) \\ \text{kJ} &= 1481 \text{ kJ} \end{split}$$



By (12), for $d_{max,e} = 17$ mm: $E_{d,p,c,Y} = [2 \cdot 5.156 \cdot 2 \cdot (17-1.96)]$ J = 310 J = 0.31 kJ By (13): $E_{d,p,t,Y} = (11 \cdot 0.31)$ kJ = 3.41 kJ By (14b): $n_{p,Y} = E_{d,Y}/E_{d,p,t,Y} = 434$

It is noted that the $S_{D,X}(T_{IN,X}) = 159.4 \text{ mm}$ and $S_{D,Y}(T_{IN,Y}) = 155.4 \text{ mm}$ spectral displacements are 6.8% and 5.4% smaller than the sums of the $ID_{m,X}$ and $ID_{m,Y}$ values derived from the timehistory analyses at the BDE, listed in Table 2, equal to 171 mm and 164.2 mm, respectively. At the same time, by multiplying the $S_{A,X}(T_{IN,X}) = 0.349 \text{ g}$ and $S_{A,Y}(T_{IN,Y}) = 0.358 \text{ g}$ spectral accelerations by g and the seismic mass M, the following base shear values are obtained: $S_{A,X}(T_{IN,X}) \cdot g \cdot M = 5736 \text{ kN}, S_{A,Y}(T_{IN,Y}) \cdot$ $g \cdot M = 5884 \text{ kN}$, which are 3.9% and 5% smaller than the corresponding $V_{m,X} = 5967 \text{ kN}, V_{m,Y} = 6,193 \text{ kN}$ values reported in Table 2 for the ground storey at the BDE. These small differences are related to the higher mode contributions to the time-history response of the structure, as compared to the first mode-based spectral evaluation assumed in the preliminary sizing procedure.

The similar total numbers of plates in X (479) and Y (434) obtained from its application is a consequence of the similar modal properties of the structure in the two directions. In order to preserve

this similarity also in retrofitted conditions, an equal design number of plates in *X* and *Y*, $n_{pd,X}$, $n_{pd,Y}$, is adopted as final output of the procedure, nearly equal to the mean of $n_{p,X}$ and $n_{p,Y}$, namely $n_{pd,X} = n_{pd,Y} = 464$.

4.2 Design of the dissipative bracing system

Based on these total numbers of plates, the final design of the protective system is carried out by: 1) selecting the vertical alignments where the dissipative braces are to be inserted, and 2) distributing the plates in elevation along the storeys. In order to minimize the architectural impact of the intervention on the interiors of the building (Martinez-Romero, 1993; Mazza, 2014), as well as to increase the torsional stiffness of the building in plan (Terenzi et al., 2020; Kookalani et al., 2022), the following 16 (8 in *X* and 8 in *Y*) alignments are chosen, as highlighted in Figure 7: 1/A-2/A, 2/A-3/A, 4/A-5/A, 5/A-6/A, 1/D-2/D, 2/D-3/D, 4/D-5/D, 5/D-6/D, in *X*; and 1/A-1/B, 1/C-1/D, 3/A-3/B, 3/C-3/D, 4/A-4/B, 4/C-4/D, 6/A-6/B, 6/C-6/D, in *Y*. Among these alignments, 12 are situated on the building perimeter, two on the stairwell perimeter and two in the interiors (3/A-3/B, 4/A-4/B).

The numbers of plates to be installed on the various storeys are fixed in proportion to the inter-storey drift profiles reported in Table 3, so as to provide a response capacity proportional to the demand highlighted by the seismic assessment analysis in current conditions. Thus, they result as follows, both in X and Y: 12 plates on the ground storey, 14 on the first, 14 on the second, 10 on the third and 8 on the fourth, for a total of 58 plates per vertical alignment (by multiplying this number by the 8 alignments per axis, the $n_{pd,X} = n_{pd,Y} = 464$ total numbers of plates are obtained). No plates are installed on the upper storey, because of the elastic response of its structural members and the small drift values up to the MCE. However, traditional non-dissipative braces are mounted on this storey, so as to prevent discontinuities in the lateral stiffness of the structure along the height of the building. A 4.6 mm-thick circular tubular section with 150 mm diameter is adopted for the steel braces at all storeys.

Front views along the A and 1 horizontal fixed lines of the structure equipped with the protective system, and installation details of the latter in a frame span are shown in Figure 8, and a view of the finite element model including the dissipative braces in Figure 9.

4.3 Performance assessment in retrofitted conditions

The modal analysis in retrofitted conditions highlights two main translational modes in this case too, whose shapes are shown in Figure 9, with vibration periods reduced to 0.609 s in *X* and 0.614 s in *Y*, and effective modal masses of 83.2% and 81.9%, and a first rotational mode around *Z*, with period and mass equal to 0.53 s and 80.7%. Like in current state, nine modes are needed to activate summed modal masses greater than 90% of the total seismic mass along *X* and *Y*, and around *Z*, whereas twenty-one modes—instead of eighteen—are needed to reach 99% of *M*. The two main translational periods are slightly greater than the $T_{FIN,X} = 0.584$ s and $T_{FIN,Y} = 0.591$ s values computed in the pre-sizing stage, with differences of 4.3% (*X*) and 3.9% (*Y*).

The Wen (1976) plasticity model, included in the library of SAP2000NL software, was assigned to the non-linear link elements adopted to simulate the response of the T-ADAS dampers in the time-history analyses. The results of the latter are recapitulated in the bottom halves of Tables 2, 3. Concerning storey shears (Table 2), reductions ranging from about 5% to 15% (SDE), 16%–23% (BDE) and 21%–31% (MCE) are noted when passing from original to retrofitted conditions. The growth of benefits in the transition from the lowest to the highest earthquake level is a consequence of the corresponding growth in the energy dissipated by the dampers. These data highlight that the latter compensates for—and even appreciably overcomes—the increase of shears caused by the stiffening effects of the protective system, as targeted by the sizing criterion.

The reductions in the stress states of columns and beams are significantly greater than the reductions in terms of storey shears. Indeed, as observed in Section 2, a significant portion of the latter is absorbed by the diagonal braces. The additional axial forces generated in the columns belonging to the alignments in plan where the system is installed, as well as the corresponding vertical forces transferred by the ground storey columns to the foundations, are all safely absorbed. As a consequence of the induced braced frame response mechanism to lateral forces and the supplementary damping action of the protective

system, only 6% of columns and 6% of beams at the BDE, and 10% of columns and 9% of beams at the MCE are in unsafe conditions after retrofit, all situated on the ground storey. By way of example, the BDErelated M_1 - M_2 biaxial moment curves for the columns situated on the 2/B vertical fixed line, shown in Figure 6 in current state, are duplicated in Figure 10 for retrofitted conditions. All response curves are limited within relevant safe domains, except for the ground storey column, where the demand/capacity ratio reaches a maximum value of 1.25. Similar results are obtained for the remaining ground storey columns in unsafe conditions (located on the 2/C, 3/A, 3/B, 3/C, 4/A, 4/B, 4/C, 5/B, 5/C lines, in addition to 2/B). The beams in unsafe conditions are the ones connecting these columns, with maximum demand/capacity ratios equal to 1.18 for bending moment, and 1.23 for shear. Thus, minimal local strengthening interventions are needed on these ground storey members, which consist in bonding single sheets of carbon fiber reinforced fabrics.

The results in terms of drifts (Table 3) highlight that the target value of 0.5% *IH* is met on all storeys at the BDE, except for the first one, where it is marginally exceeded (0.51% in *X*, and 0.52% in *Y*). A satisfactory response is obtained up to the MCE, with peak drifts of 0.64% (*X*) and 0.66% (*Y*) on the same storey, and values below or equal to 0.5% *IH* on the ground, fourth and fifth storey.

The BDE-related response cycles of the dampers installed in the 2/ D-3/D (parallel to X) and 1/C-1/D (parallel to Y) alignments are plotted in Figures 11, 12. By computing the energies dissipated by the dampers in their widest response cycles and the energies dissipated in all remaining cycles, the latter result to be equal to about 10.6 (2/D-3/D alignment dampers) and 11.2 (1/C-1/D alignment dampers) times the former. Similar values are calculated for all the remaining system alignments due to the substantial regularity of the building in plan and elevation, which determines slight seismic torsion effects. These data are well related to the value 10 assumed in the design expression (13), which underestimates the average values computed for the dampers situated in all alignments by about 10%. Concerning this estimate, it should be noted that the energy contribution associated with the secondary cycles is a function of the type of input ground motions assumed in the analysis. Indeed, a value approximately equal to 10 is well suited for artificial accelerograms generated from normative response spectra, like the ones used in this study, characterized by a considerable number of acceleration peaks with comparable amplitude to the widest peak. In the case of real ground motion records, the secondary peaks tend to be smaller. Therefore, the ratio of the energy dissipated in the secondary cycles to the one dissipated in the widest response cycle approximately ranges from 4 to 7, depending on several seismological, subsoil and building site factors (Sorace et al., 2016). This must be properly taken into account upon applying Eq. 13 when real ground motions, instead of artificial accelerograms, are used as input in the assessment analysis.

By computing the total energy dissipated by the 464 + 464T-ADAS dampers, a value of 2489 kJ results at the BDE, i.e., 19.8% smaller than the sum of the $E_{d,X}$ = 1632 kJ and $E_{d,Y}$ = 1481 kJ values estimated by means of relation (11) in the sizing process, equal to 3103 kJ. This difference is motivated by the fact that the maximum displacements achieved in the response cycles of the dampers are nearly equal to 15 mm on the ground, first and second storey, 13 mm on the third and 8.5 mm on the fourth, that is, about 12%, 24%, and 50% smaller than the tentatively assumed $d_{max,e} = ID_{m,t}$ value, respectively. The resulting average 22% overestimation of peak displacements in the storeys is only partially compensated by about 10% underestimation of the

dissipated energy contribution supplied by the secondary cycles, resulting in the above-mentioned approximate 20% overestimation yielded by the $E_{d,X}$, $E_{d,Y}$ values.

5 Conclusion

The use of supplementary damping devices with high elastic stiffness requires, unlike pure dampers or low-stiffness dampers, proper control of the stiffening effects produced by their installation in dissipative bracing systems adopted as retrofit measure for existing frame structures. This is the case of ADAS dampers, the elastic stiffness of which is normally so high that the system behaves like a corresponding traditional bracing system up to the first plasticization of the devices.

A sizing procedure for ADAS dampers aimed at expressly controlling the stiffening effects involved in their application is offered in this study, whose conceptual and practical implications are summarized below.

- The procedure allows estimating the energy dissipation capacity to be assigned to the protective system by means of simple analytical relations making use of spectral displacement, velocity and pseudo-acceleration ordinates.
- As the energy dissipation preliminary estimate is obtained by means of a single linear analytical relation, the procedure is intrinsically not iterative. This marks a distinction as compared to sizing criteria based on non-linear expressions or trial-anderror tentative approaches.
- The damping action of the ADAS devices is calibrated in order to generate a prefixed pseudo-acceleration drop, $\Delta S_{A-,diss}$, compensating for the corresponding rise, ΔS_{A+} , induced by the stiffening effects of the intervention.
- This compensation is modulated by means of the m_{ed} energy dissipation demand coefficient to be calibrated on the design objectives formulated in terms of base shear, for which a value smaller than 1 can be selected in the case of essentially regular structures, so as to avoid excessive supplementary damping additions.
- This assumption, as well as the ones concerning the remaining parameters required to initialize the sizing process (the $d_{max,e}$ maximum displacement of the damper plates, and the $E_{d,p,c}$ total energy dissipated by the plates in the cycles with smaller amplitude than the widest cycle) are substantially validated for the examined frame building by the results of the non-linear time-history analyses carried out in the final verification stage.
- The latter results also satisfactorily meet the preliminarily estimated base shear and inter-storey drift demands.
- At the same time, energy demand is overestimated by about 20%, since while the estimated maximum damper displacements are nearly reached on the three lower storeys, where the peak response displacements are at most 12% smaller than the tentatively assumed $d_{max,e} = ID_{m,t}$ value, the differences reach about 24% and 50% on the third and fourth storey.
- Although this may suggest the need to further reduce the number of plates on these two storeys, as compared to the lower storeys, the exploitation of the energy dissipation capacities of the dampers is similar at all levels. This confirms the drift-proportional variation of the number of

plates along the height of the structure as an acceptable choice at the sizing stage.

- Based on these results, in order to approximate better the maximum damper displacement demand for taller frame buildings than the case study one, it can be suggested to assume $d_{max,e} = ID_{m,t}$ for the storeys belonging to their bottom half, and a progressively decreasing value along the height (e.g., ranging from about 0.8 to 0.5 $ID_{m,t}$) for the remaining storeys where the system is installed.
- Thanks to the balanced contributions of the stiffening and damping effects added by the dissipative braces, a satisfactory seismic performance improvement of the case study building is achieved in retrofitted conditions; this is assessed by the peak drifts practically constrained below the Immediate Occupancy-related 0.5% *IH* limitation at the BDE (and no greater than 0.66% peak values at the MCE), and the small number of frame members in slightly unsafe state (6% of columns and 6% of beams at the BDE, and 10% of columns and 9% of beams at the MCE). For these members, minimal local strengthening interventions based on the application of carbon fiber reinforced fabrics are suggested, as an alternative to a more expensive increase in the number of plates of the T-ADAS devices.

Data availability statement

The raw data supporting the conclusions of this article will be made available by the authors, without undue reservation.

Author contributions

GT and SS equally contributed to the conception of the study and formulation of the sizing design procedure; GT, SS, and EF equally contributed to the development of numerical analyses, elaboration, and interpretation of results, and preparation of the draft manuscript.

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Conflict of interest

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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References

Aiken, I. D., Nims, D. K., Whittaker, A. S., and Kelly, J. M. (1993). Testing of passive energy dissipation systems. *Earthq. Spectra* 9 (3), 335–370. doi:10.1193/1.1585720

Akehashi, H., and Takewaki, I. (2021). Ideal drift response curve for robust optimal damper design for elastic-plastic MDOF structures under multi-level earthquakes. *Comput. Model. Eng. Sci.* 129 (3), 1181–1207. doi:10.32604/cmes.2021.017204

Aloisio, A., Rosso, M. M., Iqbal, A., and Fragiacomo, M. (2022). Hysteresis modeling of timber-based structural systems using a combined data and model-driven approach. *Comput. Struct.* 269 (3), 106830. doi:10.1016/j.compstruc.2022.106830

ASCE (2017). ASCE/SEI 41-17 – seismic evaluation and retrofit of existing buildings. Reston, VA: ASCE-American Society of Civil Engineers – Structural Engineering Institute.

ASCE (2000). Fema 356 – prestandard and Commentary for the seismic rehabilitation of buildings. Reston, VA: ASCE-American Society of Civil Engineers.

ATC (2003). ATC 58-2. Preliminary evaluation of methods for defining performance. Redwood City, CA: ATC-Applied Technology Council.

Bergman, D. M., and Goel, S. C. (1987). Evaluation of cyclic testing of steel-plate devices for added damping and stiffness. Report UMCE 87-10. Ann Arbor, MI: Department of Civil Engineering, University of Michigan.

Boggian, F., Tardo, C., Aloisio, A., Marino, E. M., and Tomasi, R. (2022). Experimental cyclic response of a novel friction connection for seismic retrofitting of RC buildings with CLT panels. *ASCE J. Struct. Eng.* 148 (5), 04022040. doi:10.1061/(ASCE)ST.1943-541X.0003313

CSI (2022). SAP2000NL. Theoretical and user's manual. Release 23.07. Berkeley, CA: Computers & Structures Inc.

Dargush, G. F., and Soong, T. T. (1995). Behavior of metallic plate dampers in seismic passive energy dissipation systems. *Earthq. Spectra* 11 (4), 545–568. doi:10.1193/1.1585827

De Domenico, D., and Hajirasouliha, I. (2021). Multi-level performance-based design optimisation of steel frames with nonlinear viscous dampers. *Bull. Earthq. Eng.* 19, 5015–5049. doi:10.1007/s10518-021-01152-7

Di Trapani, F., Malavisi, M., Marano, G. C., Sberna, A. P., and Greco, R. (2020). Optimal seismic retrofitting of reinforced concrete buildings by steel-jacketing using a genetic algorithmbased framework. *Eng. Struct.* 219, 110864. doi:10.1016/j.engstruct.2020.110864

Fardis, M. N. (2007). Guidelines for displacement-based design of buildings and bridges. LESSLOSS Report No. 2007/05. Pavia, Italy: IUSS Press, 231. ISBN: 978-88-6198-009-9.

Gandelli, E., De Domenico, D., and Quaglini, V. (2021). Cyclic engagement of hysteretic steel dampers in braced buildings: A parametric investigation. *Bull. Earthq. Eng.* 19, 5219–5251. doi:10.1007/s10518-021-01156-3

Greco, R., and Marano, G. C. (2016). Optimum design of viscous dissipative links in wall-frame systems. *Struct. Des. Tall Special Build.* 25 (9), 412–428. doi:10.1002/tal.1265

Italian Ministry of Infrastructure and Transport (2018). Update of technical Standards for constructions. Rome, Italy: D.M. 17-01-2018(in Italian).

Khoshkalam, M., Mortezagholi, M. H., and Zahrai, S. M. (2022). Proposed modification for ADAS damper to eliminate axial force and improve seismic performance. *J. Earthq. Eng.* 26 (10), 5130–5152. doi:10.1080/13632469.2020.1859419

Kookalani, S., Shen, D., Zhu, L. L., and Lindsey, M. (2022). An overview of optimal damper placement methods in structures. *Iran J. Sci. Technol. Trans. Civ. Eng.* 46, 1785–1804. doi:10.1007/s40996-021-00752-2

Lavan, O., and Dargush, G. F. (2009). Multi-objective evolutionary seismic design with passive energy dissipation systems. *J. Earthq. Eng.* 13, 758–790. doi:10.1080/13632460802598545

Lu, W. T., and Phillips, B. M. (2022). A fundamental-period-preserving seismic retrofit methodology for low-rise buildings with supplemental inerters. *Eng. Struct.* 266, 114583. doi:10.1016/j.engstruct.2022.114583

Marano, G. C., Trentadue, F., and Greco, R. (2007). Stochastic optimum design criterion of added viscous dampers for buildings seismic protection. *Struct. Eng. Mech.* 25 (1), 21–37. doi:10.12989/sem.2007.25.1.021

Martinez-Romero, E. (1993). Experiences on the use of supplementary energy dissipators on building structures. *Earthq. Spectra* 9 (3), 581-625. doi:10.1193/1. 1585731

Mazza, F. (2014). Displacement-based seismic design of hysteretic damped braces for retrofitting in-plan irregular r.c. framed structures. *Soil Dyn. Earthq. Eng.* 66, 231–240. doi:10.1016/j.soildyn.2014.07.001

Mazza, F., and Imbrogno, G. (2019). Effects of fire duration on the seismic retrofitting with hysteretic damped braces of r.c. school buildings. *Front. Built Environ.* 5, 141. doi:10. 3389/fbuil.2019.00141

Moghaddasi, M., and Namazi, A. (2016). Assessment of performance of TADAS dampers for the seismic rehabilitation of buildings. *Int. J. Appl. Eng. Res.* 11 (21), 10516–10523. doi:10.37622/010516

Mohammadi, R. K., Nasri, A., and Ghaffary, A. (2017). TADAS dampers in very large deformations. Int. J. Steel Struct. 17, 515–524. doi:10.1007/s13296-017-6011-y

Priestley, M. J. N., and Calvi, G. M. (1997). "Concepts and procedures for direct displacement-based design and assessment," in *Seismic design methodologies for the next generation of codes* (UK: Routledge), 11. ISBN: 9780203740019-16

Priestley, M. J. N., Calvi, G. M., and Kowalsky, M. J. (2007). Displacement-based seismic design of structures. Pavia, Italy: IUSS Press, 721. ISBN: 978-88-6198-0006.

Priestley, M. J. N. (1997). Displacement-based seismic assessment of existing reinforced concrete buildings. *J. Earthq. Eng.* 1, 157–192. doi:10.1080/13632469708962365

SEAOC (1995). "Performance-based seismic engineering." in. Vision 2000 committee. Sacramento, CA: Structural Engineers Association of California.

Shojaeifar, H., Maleki, A., and Lotfollahi-Yaghin, M. A. (2020). Performance evaluation of curved-TADAS damper on seismic response of moment resisting steel frame. *Int. J. Eng.* 33 (1), 55–67. doi:10.5829/ije.2020.33.01a.07

Sorace, S., Terenzi, G., and Mori, C. (2016). Passive energy dissipation-based retrofit strategies for R/C frame water towers. *Eng. Struct.* 106, 385–398. doi:10.1016/j.engstruct. 2015.10.038

Terenzi, G., Costoli, I., and Sorace, S. (2020). Activation control extension of a design method of fluid viscous dissipative bracing systems. *Bull. Earthq. Eng.* 18 (8), 4017–4038. doi:10.1007/s10518-020-00849-5

Teruna, D. R., Majid, T. A., and Budiono, B. (2015). Experimental study of hysteretic steel damper for energy dissipation capacity. *Appl. Sci.* 2015, 1–12. doi:10.1155/2015/631726

Tsai, K. C., Chen, H. W., Hong, C. P., and Su, Y. F. (1993). Design of steel triangular plate energy absorbers for seismic-resistant construction. *Earthq. Spectra* 9 (3), 505–528. doi:10. 1193/1.1585727

Wen, Y. K. (1976). Method for random vibration of hysteretic systems. ASCE J. Eng. Mech. Div. 102 (1022), 249–263. doi:10.1061/JMCEA3.0002106

Whittaker, A. S., Bertero, V. V., Thompson, C. L., and Alonso, L. J. (1991). Seismic testing of steel plate energy dissipation devices. *Earthq. Spectra* 7 (4), 563–604. doi:10. 1193/1.1585644

Zhao, J., Sun, J., and Qiu, H. (2022). Rapid seismic retrofit of damaged RC frames using gapped eccentric steel brace system equipped with dampers. *J. Build. Eng.* 53, 104532. doi:10.1016/j.jobe.2022.104532