

Origin of neutron-capture elements with the Gaia-ESO survey: the evolution of s- and r-process elements across the Milky Way

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ABSTRACT

We investigate the origin of neutron-capture elements by analysing their abundance patterns and radial gradients in the Galactic thin disc. We adopt a detailed two-infall chemical evolution model for the Milky Way, including state-of-the-art nucleosynthesis prescriptions for neutron-capture elements. We consider r-process nucleosynthesis from merging neutron stars (MNS) and magneto-rotational supernovae (MR-SNe), and s-process synthesis from low- and intermediate-mass stars (LIMS) and rotating massive stars. The predictions of our model are compared with data from the sixth data release of the *Gaia*-ESO survey, from which we consider 62 open clusters with age $\gtrsim 0.1$ Gyr and ~ 1300 Milky Way disc field stars. We conclude that: (i) the [Eu/Fe] versus [Fe/H] diagram is reproduced by both prompt and delayed sources, with the prompt source dominating Eu production; (ii) rotation in massive stars significantly contributes to the first peak s-process elements, but MNS and MR-SNe are necessary to match the observations; and (iii) our model slightly underpredicts Mo and Nd, while accurately reproducing the [Pr/Fe] versus [Fe/H] trend. Regarding the radial gradients, we find that: (i) our predicted [Fe/H] gradient slope agrees with observations from *Gaia*-ESO and other high-resolution spectroscopic surveys; (ii) the predicted [Eu/H] radial gradient slope is steeper than the observed one, regardless of how quick the production of Eu is, prompting discussion on different Galaxy-formation scenarios and stellar radial migration effects; and (iii) elements in the second s-process peak as well as Nd and Pr exhibit a plateau at low-Galactocentric distances, likely due to enhanced enrichment from LIMS in the inner regions.

Key words: nuclear reactions, nucleosynthesis, abundances – stars: neutron – stars: rotation – supernovae: general – Galaxy: abundances – Galaxy: evolution.

1 INTRODUCTION

The majority of elements beyond the Fe peak are produced by neutron-capture processes which can be rapid (*r-process*) or slow (*s-process*) with respect to the β -decay of the nuclei. Understanding which are the astrophysical sites of these two processes has become one of the major challenges in stellar physics and chemical evolution.

The r-process sites, in particular, are still under debate, with possible main producer candidates being supernovae (SNe) or merging of compact objects (neutron stars or neutron star-black hole, e.g. Thielemann et al. 2017; Cowan et al. 2021). Historically, the occurrence of the r-process has first been associated with core-collapse supernovae (CC-SNe; Woosley et al. 1994). However, during recent years it has been shown that hydrodynamical simulations of the neutrino-driven wind are not able to reach the extreme conditions necessary for the r-process (Arcones & Thielemann 2013).

In addition to the neutrino-driven wind, a second mechanism has been proposed in order to explain observations of very energetic explosions. This mechanism relies on rapid rotation of the Fe core from which rotational energy can be extracted via a strong magnetic field. SNe explosions which may rely on that mechanism are named magneto-rotational supernovae (MR-SNe, see e.g. Winteler et al. 2012; Nishimura, Takiwaki & Thielemann 2015; Nishimura et al. 2017; Reichert et al. 2021, 2023). MR-SNe are rare with respect to normal CC-SNe, since the required rotation rates and high magnetic fields restrict the mechanism to a minority of progenitor stars (only 1 per cent of stars with initial mass larger than $10 M_{\odot}$, according to Woosley & Heger 2006). Despite their low rate, MR-SNe may be important contributors to the enrichment of galaxies with heavy elements (see Arcones & Thielemann 2023 for a recent review), especially at low metallicities. However, the dependence of their nucleosynthesis on the magnetic field is strong and only with high magnetic fields the r-process produces heavy elements up to the third r-process peak (Reichert et al. 2021) and still more work is needed to get a much better picture (see also Schatz et al. 2022).

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Thanks to the detection of the kilonova AT2017gfo associated with the gravitational wave event GW170817 (Abbott et al. 2017), merging neutron stars (MNS) have been proven to be a primary site for the production of r-process material (Pian et al. 2017). Watson et al. (2019) reported the identification of the neutron-capture element Sr in the reanalysis of the spectra and Perego et al. (2022) computed the amount of Sr synthesized in the wind ejecta of MNS and found it to be consistent with the one required to explain the spectral features of AT2017gfo. However, although the observations point towards MNS as the major astrophysical r-process site, chemical evolution simulations still struggle to reproduce the abundance pattern of the [Eu/Fe] versus [Fe/H] (with Eu being a typical r-process element) if MNS are the only producers of r-process material and realistic time-scales for merging are assumed. In chemical evolution simulations, the time-scales for the production of a certain chemical element are of great importance. For MNS the delay time for the coalescence is determined by the stellar nuclear lifetime and the delay due to gravitational radiation. Therefore, since the delay time can potentially assume a wide range of values, the time-scales for the enrichment from MNS will depend on a delay time distribution (DTD, see Simonetti et al. 2019; Greggio, Simonetti & Matteucci 2021). Matteucci et al. (2014) showed that the observed [Eu/Fe] abundance pattern in the Milky Way (MW) can be reproduced with only MNS as Eu producers if the time-scale for the Eu pollution does not exceed 10–30 Myr, which can be attained by assuming a gravitational delay of 1 Myr on top of the nuclear evolution time-scale of the progenitors. If longer delays are assumed then another source of Eu should be included, especially at low metallicities. A large number of works (e.g. Wehmeyer, Pignatari & Thielemann 2015; Côté et al. 2019; Simonetti et al. 2019; Kobayashi, Karakas & Lugaro 2020; Cavallo, Cescutti & Matteucci 2021; Molero et al. 2021a) point towards a scenario in which both a quick source and a delayed one produce r-process material. The delayed source is represented by MNS with a DTD while the quick source is usually represented by massive stars (e.g. MR-SNe). In such a way, the lack of Eu from MNS at low [Fe/H], due to longer delay times for merging, is compensated by the production from MR-SNe. However, if these sources are active also for the production of the r-process component of Ba, then the above models struggle to reproduce the observed [Ba/Fe] versus [Fe/H] trend at low metallicities (see Molero et al. 2021b), suggesting that more investigation is needed.

Conversely, we have a better understanding of the formation sites for the s-process. The s-process can be decomposed into three sub-processes: (i) the weak s-process, mainly responsible for the production of the first peak s-process elements (Y, Sr, and Zr); (ii) the main s-process which produces elements belonging to the second s-process peak (Ba, La, and Ce); and (iii) a strong s-process responsible for the production of the third s-process peak elements (Pb, Au, and Bi). Rotating massive stars are the main responsible for the production of the weak s-process. The source of neutrons is the reaction $^{22}\text{Ne}(\alpha, n)^{25}\text{Mg}$ which takes place mainly during core He- and C-burning phases (Pignatari et al. 2010; Frischknecht et al. 2016; Limongi & Chieffi 2018). The main s-process component occurs in low- and intermediate-mass stars (LIMS; $M < 8 M_{\odot}$) during their asymptotic giant branch (AGB) phase, in which the neutron source is the reaction $^{13}\text{C}(\alpha, n)^{16}\text{O}$ (Karakas 2010; Fishlock et al. 2014; Cristallo et al. 2015). Finally, low-metallicity low-mass AGB stars are responsible for the production of elements belonging to the third s-process peak through the strong s-process.

In this paper, we aim at improving our understanding of the origin of the neutron-capture elements. For this purpose, we study both the

abundance patterns and the radial gradients of five s-process (Y, Zr, Ba, La, and Ce) and four mixed-/r-process elements (Eu, Mo, Nd, and Pr) in the Galactic thin disc. We take advantage of the sixth data release (DR) of the *Gaia*-ESO survey from which our sample has been collected. The sample consists of 62 open clusters (OCs) located between ~ 5 and 20 kpc in Galactocentric distances, with ages from 0.1 to 7 Gyr and covering a metallicity range of $-0.5 < [\text{Fe}/\text{H}] < 0.4$ dex, together with ~ 1300 MW disc field stars in the metallicity range of $-1.5 < [\text{Fe}/\text{H}] < 0.5$ dex [see also Magrini et al. 2023 (hereafter M23); Van der Swaelmen et al. 2023]. We adopt a detailed two-infall chemical evolution model with an inside-out scenario of formation, extensively tested to explain the features observed in the MW disc (e.g. Palla et al. 2020; Spitoni et al. 2021). With our model, we are able to follow the evolution of 40 different chemical species.

The paper is structured as follows. In Section 2, we present the *Gaia*-ESO sample. In Section 3 and 4, we describe the details of the chemical evolution model. Section 5 presents our results first for the [El/Fe] versus [Fe/H] and then for the radial gradients of both [Fe/H] and the neutron-capture elements. Finally, in Section 6, we draw our summary and conclusions.

2 OBSERVATIONAL DATA

The *Gaia*-ESO survey is a large public spectroscopic survey that observed for 340 nights at the VLT from the end of 2011 to 2018 using the FLAMES spectrograph (Gilmore et al. 2022; Randich et al. 2022). During the survey, FLAMES was used at intermediate spectral resolution with GIRAFFE, and at high resolution with UVES. In this work, we select the spectra of FGK stars obtained with UVES at $R = 47\,000$, covering the spectral range 480.0–680.0 nm. The spectra were analysed by the *Gaia*-ESO Working Group (WG 11) dedicated to the analysis of FGK stars. We refer the reader to Randich et al. (2022) and Gilmore et al. (2022) for a general description of the structure of *Gaia*-ESO and of the analysis procedure. The final catalogue containing among others atmospheric parameters, elemental abundances, and radial and projected rotational velocities is publicly available in the ESO archive.¹ The high spectral resolution of UVES and the large collecting area of VLT make it possible to obtain precise abundances of many neutron-capture elements: the slow-process elements Y, Zr, Ba, La, and Ce, and the mixed-/r-process elements Mo, Pr, Nd, and Eu. Throughout the paper, we use these abundances, normalizing them to the Solar scale as in Viscasillas Vázquez et al. (2022) and M23.

Other surveys as the Apache Point Observatory Galactic Evolution Experiment (APOGEE-1 and APOGEE-2; Majewski et al. 2017) and the Galactic Archaeology with HERMES (GALAH; De Silva et al. 2015) are providing abundances of some neutron-capture elements as well. For example, APOGEE provides for a limited percentage of stars abundances of Ge, Rb, Ce, Nd, and Yb, but only Ce has been used in scientific works (Cunha et al. 2017; Donor et al. 2020). Recently, Hayes et al. (2022) explored weak and blended species in the APOGEE data base, providing also new and improved abundances of Ce and Nd. The GALAH survey provided in its DR3 (Buder et al. 2021) abundances of several neutron-capture elements, namely Y, Ba, La, Rb, Mo, Ru, Nd, Sm, and of Eu. However, their accuracy is often limited because of the lower spectral resolution.

¹<https://www.eso.org/qi/catalogQuery/index/393>

The quality of the neutron-capture abundances in the UVES spectra of *Gaia*-ESO remains, thus, unrivalled.

2.1 The data samples

In this work, we used two different samples of stars: a first sample composed by stars that are members of OCs, and a second sample of field stars. For the former, we benefit of the large sample of stars members of open star clusters, located at various Galactocentric distances and covering a wide age range, from a few million years to about 7 Gyr. Star clusters, containing groups of coeval and chemically homogeneous stars, allow, indeed, a more accurate determination of age and chemical properties with respect to field stars. The latter is, instead, composed of stars of the main-sequence turn-off (MSTO) (see Stokutè et al. 2016, for the description of the selection function).

2.1.1 The sample of OCs

In this paper, we consider among the sample of OCs observed by *Gaia*-ESO, the 62 clusters older than 100 Myr, as done in M23. The motivation is twofold: Younger stars might be affected by problems in the spectral analysis, as shown by (Baratella et al. 2020, 2021; Spina et al. 2021); young clusters represent only the last moments of global galactic chemical evolution, with negligible variations of the abundance with respect to the overall time-scale. The distribution in age and distances of our sample OCs is given in Viscasillas Vázquez et al. (2022, see their fig. 1). For each cluster, we considered the average abundances of its member stars. The membership analysis is performed as in Viscasillas Vázquez et al. (2022), based on three-dimensional kinematics, complementing the radial velocities from *Gaia*-ESO with proper motions and parallaxes from *Gaia* DR3 (Gaia Collaboration 2021). Ages and Galactocentric distances are homogeneously derived with *Gaia* DR2 data in Cantat-Gaudin et al. (2020). In the paper, we use the OC sample to trace the abundance radial gradients, and thanks to the wide age range, also their evolution over time.

2.1.2 The sample of field stars

The sample of field stars is composed, as in Viscasillas Vázquez et al. (2022), by stars selected through the GES_FLD keywords related to the field stars (GES_MW for general MW fields, GES_MW_BL for fields in the direction of the Galactic bulge, GES_K2 for stars observed in *Kepler*2 fields, GES_CR for stars observed in *CoRoT* fields, and benchmark stars GES_SD), and stars which are non-members of OCs. We combined the two samples, applying a further selection on the signal-to-noise ratio (SNR) and on the uncertainties on the stellar parameters: $\text{SNR} > 20$; $\sigma T_{\text{eff}} < 150$ K, $\sigma \log g < 0.25$, $\sigma [\text{Fe}/\text{H}] < 0.20$, and $\sigma \xi < 0.20$ km s^{-1} . A final selection was introduced considering only stars with at least one measurement of the abundances of one of the considered neutron-capture elements, and with an uncertainty $eA(EI) < 0.1$. These selections produce a sample of approximately 1300 stars. Due to the selection function of the *Gaia*-ESO survey (see Stokutè et al. 2016), this sample is dominated by stars at the MSTO, with some giant stars which are non-members of OCs. Due to the wide metallicity range covered by the field stars, we use them to study the evolution in the $[\text{El}/\text{Fe}]$ versus $[\text{Fe}/\text{H}]$ planes.

3 THE MODEL

The adopted chemical evolution model derives from the two-infall model originally developed by Chiappini, Matteucci & Gratton (1997). Here, we use the revised version of Palla et al. (2020) focusing our study on the thick and thin discs only, without taking into account the evolution of the Galactic halo.

The two-infall model assumes that the Galaxy forms as a result of two infall episodes. The first one forms the thick disc while the second one, delayed with respect to the first, is responsible for the creation of the thin disc. The composition of the infalling gas is assumed to be primordial. The disc is approximated by independent rings 2 kpc wide.

The basic equations which describe the evolution of the fraction of gas mass in the form of a generic element i , G_i , are (see Matteucci 2012)

$$\dot{G}_i(R, t) = -\Psi(R, t)X_i(R, t) + R_i(R, t) + \dot{G}_{i,\text{inf}}(R, t). \quad (1)$$

The first term on the right-hand side of the equation represents the rate at which the chemical elements are subtracted to the interstellar medium (ISM) to be included in stars. $X_i(R, t)$ represents the abundance by mass of a given elements i , while $\Psi(R, t)$ is the star-formation rate (SFR), here parametrized according to the Schmidt–Kennicutt law (Kennicutt 1998):

$$\Psi(R, t) \propto \nu \sigma_{\text{gas}}(R, t)^k, \quad (2)$$

where σ_{gas} is the surface gas density, $k = 1.5$ is the law index, and ν is the star-formation efficiency expressed in Gyr^{-1} . This last term is assumed to vary with the Galactocentric distance as in Palla et al. (2020).

The second term, $R_i(R, t)$, represents the fraction of matter that is restored to the ISM in the form of the element i through stellar winds, SN explosions, novae, and MNS. Namely, it represents the rate at which chemical elements are restored to the ISM by all stars dying at the time t . It depends also on the initial mass function (IMF), which here is the Kroupa, Tout & Gilmore (1993)'s one.

The last term in equation (2) is the gas accretion rate. In the two-infall model, it is computed in the following way:

$$\dot{G}_{i,\text{inf}}(R, t) = A(R)X_{i,\text{inf}}e^{-t/\tau_1} + \theta(t - t_{\text{max}})B(R)X_{i,\text{inf}}e^{-(t-t_{\text{max}})/\tau_2}, \quad (3)$$

where $G_{i,\text{inf}}(R, t)$ is the infalling material in the form of the elements i and $X_{i,\text{inf}}$ is the composition of the infalling gas, here assumed to be primordial. τ_1 and $\tau_2(R)$ are the infall time-scales for the thick and thin discs, respectively. We fix $\tau_1 = 1$ Gyr and let τ_2 vary with the radius according to the inside-out scenario (e.g. Matteucci & Francois 1989; Romano et al. 2000; Chiappini, Matteucci & Romano 2001) as

$$\tau_2(R) = \left(1.033 \frac{R}{\text{kpc}} - 1.267\right) \text{Gyr}. \quad (4)$$

t_{max} is the time for the maximum infall on to the thin disc and it corresponds to the end of the thick disc phase and the start of the second infall episode. The typical value assumed for t_{max} in previous models (e.g. Chiappini et al. 2001; Spitoni et al. 2009; Romano et al. 2010; Grisoni, Spitoni & Matteucci 2018) is ~ 1 Gyr. However, more recent works found out that the gap between the formation of the two discs should be higher in order to reproduce both stellar abundance constraints and ages. Here, we follow the prescriptions adopted in Palla et al. (2020), who found a best value of $t_{\text{max}} \simeq 3.25$ Gyr (in agreement with Spitoni et al. 2019, 2020).

The parameters $A(R)$ and $B(R)$ are fixed in order to reproduce the present time total surface mass densities of the thick and thin discs, as a function of the radius. Here, we assume that the surface mass densities of the discs both follow exponential laws. In particular, we adopt the following profiles for the thin and thick disc, respectively:

$$\Sigma_{\text{thin}}(R) = \Sigma_{0,\text{thin}} e^{-R/3.5}, \quad (5)$$

$$\Sigma_{\text{thick}}(R) = \Sigma_{0,\text{thick}} e^{-R/2.3}. \quad (6)$$

Where $\Sigma_{0,\text{thin}} = 531 M_{\odot} \text{pc}^{-2}$ is the central surface mass density, and $\Sigma_{0,\text{thick}}$ is fixed in order to obtain $\Sigma_{\text{thick}}(8 \text{ kpc}) = 12 M_{\odot} \text{pc}^{-2}$. As explained in Palla et al. (2020), these choices for the discs surface mass densities allow us to obtain $\Sigma_{\text{thin}}(8 \text{ kpc}) \sim 54 M_{\odot} \text{pc}^{-2}$ (in agreement with Bovy & Rix 2013 and Read 2014) and a ratio $\Sigma_{\text{thin}}(8 \text{ kpc})/\Sigma_{\text{thick}}(8 \text{ kpc}) \sim 4$ (in agreement with Spitoni et al. 2020).

4 NUCLEOSYNTHESIS PRESCRIPTIONS

For all stars sufficiently massive to die in a Hubble time, the following stellar yields have been adopted:

(i) For LIMS ($1 \leq M/M_{\odot} \leq 6$), we adopted the non-rotational set of yields available on the web pages of the FRUITY data base (Cristallo et al. 2009, 2011, 2015).²

(ii) For massive stars, we implemented Limongi & Chieffi (2018)'s recommended yield set R where mass-loss and rotation are taken into account.

(iii) For Type Ia SNe (SNeIa), we assumed the single-degenerate scenario (see Matteucci & Recchi 2001; Palla 2021 for details) for the progenitors, in which SNe arise from the explosion via C-deflagration of a CO white dwarf in a close binary system when it has almost reached the Chandrasekhar mass due to accretion from its red giant companion. The adopted stellar yields are from Iwamoto et al. (1999; model W7).

(iv) We consider also chemical enrichment from novae. They do not affect the heavy elements treated here, but they can be important for the production of ⁷Li and CNO isotopes (see José & Hernanz 2007).

4.1 Heavy elements production

All the neutron-capture elements studied in this work (apart from Eu) are assumed to be partially produced by the r- and s-processes.

The s-process nucleosynthesis takes place in LIMS during the AGB phase and in rotating massive stars, with yields specified in the previous paragraph. Neutrons are produced via the reactions ¹³C(α , n)¹⁶O and ²²Ne(α , n)²⁵Mg, with the former reaction being the dominant contribution in low-mass stars and the latter in more massive AGBs (see Cristallo et al. 2011, 2015 for details) and massive stars (Longland, Iliadis & Karakas 2012).

For the r-process nucleosynthesis, we considered two channels: MNS and MR-SNe. MNS are computed as systems of two neutron stars of $1.4 M_{\odot}$ with progenitors in the 9–50 M_{\odot} mass range. Their rate is computed as the convolution between a given DTD and the SFR, as

$$R_{\text{MNS}}(t) = k_{\alpha} \int_{\tau_i}^{\min(t, \tau_x)} \alpha_{\text{MNS}}(\tau) \Psi(t - \tau) f_{\text{MNS}}(\tau) d\tau. \quad (7)$$

k_{α} is the number of neutron-star progenitors per unit mass in a stellar generation and the α_{MNS} parameter is the fraction of stars in the

correct mass range which can give rise to a double neutron-star merging event. In principle, α_{MNS} can vary with time, but here it is assumed to be constant and it is fine-tuned in order to reproduce the latest estimation of the MNS rate of Abbott et al. (2021). The DTD represents the probability that the merging event would happen at a certain time t after the formation of the progenitor binary system. For MNS, the delay between the creation of the progenitors binary system and the merging event is the sum between the nuclear lifetime of the secondary component and the delay due to the gravitational radiation. The adopted DTD in this work is the following (for a detailed discussion see Simonetti et al. 2019; Greggio et al. 2021):

$$f_{\text{MNS}}(\tau) \propto \begin{cases} 0 & \text{if } \tau < 10 \text{ Myr} \\ p_1 & \text{if } 10 < \tau/\text{Myr} < 40 \\ p_2 \tau^{0.25\beta - 0.75} (M_m^{0.75(\beta + 2.33)} - M_M^{0.75(\beta + 2.33)}) & \\ \text{if } 40 \text{ Myr} < \tau < 13.7 \text{ Gyr} \end{cases} \quad (8)$$

with $\beta = -0.9$, M_m and M_M being the minimum and maximum total mass of the binary system and p_1 and p_2 are chosen in order to obtain a continuous and normalized function.

The yields from MNS of the various elements considered in this study have been obtained as in Molero et al. (2021b) by assuming a scaling relation between them and those of Sr. The adopted yield of Sr is equal to $Y_{\text{Sr}}^{\text{MNS}} = 1 \times 10^{-4} M_{\odot}$, which corresponds to that measured by Watson et al. (2019) in the re-analysis of the spectra of the kilonova AT2017gfo multiplied by a factor of 10 (see Molero et al. 2021b for details).

Although MR-SNe are theorized to be among the most important contributors to the enrichment of r-process material, Woosley & Heger (2006) speculated that only 1 per cent of stars with initial mass $\geq 10 M_{\odot}$ can have the necessary conditions to die as a MR-SNe. A common assumption in chemical evolution models is that only 10 per cent of all stars with initial mass in the 10–80 M_{\odot} range end their lives as MR-SNe [e.g. Cescutti & Chiappini 2014; Cescutti et al. 2015; Rizzuti et al. 2019 (hereafter R19), 2021; Molero et al. 2021b]. Both the percentage of stars, their mass range, and the yields of r-process material are free parameters in chemical evolution simulations and they are usually fine-tuned in order to reproduce the observations of abundances. In order to avoid degeneracy issues, in this work we fixed the mass range and yields, while keeping the percentage of stars as a free parameter. The mass range is reduced to 10–25 M_{\odot} in order to be consistent with the set of yields adopted for massive stars. In fact, in Limongi & Chieffi (2018)'s set R stars more massive than 25 M_{\odot} are assumed to fully collapse to a black hole and their chemical enrichment is due to the stellar winds. Therefore, in these conditions, it would be impossible for the star to develop magnetic fields strong enough to generate a MR-SNe. It must be noted that this variation in the mass range will not produce a too significant difference in the results, because of the adopted IMF (Kroupa et al. 1993), which is known to be top-light, i.e. which disfavours the presence of very massive stars due to its steep high-mass end slope. The set of yields adopted for the MR-SNe is the one of Nishimura et al. (2017), their model L0.75, chosen in order to be consistent with the best model of our previous work (Molero et al. 2021b). For some of the studied elements for which those yields predicted a much higher/lower production (Y, Zr, Mo, Nd, and Pr) they have been scaled to the one of Eu according to the solar abundances. Finally, the percentage of stars able to explode as MR-SNe has been fine-tuned in order to fit the observed [Eu/Fe] versus [Fe/H] relation (see next sections), and set to 20 per cent.

In Table 1, we summarize the adopted nucleosynthesis prescriptions.

²<http://fruity.oa-teramo.inaf.it>

Table 1. Nucleosynthesis prescriptions. In the 1st column we report the name of the model, in the 2nd the initial rotational velocities for massive stars. In the 3rd, 4th, and 5th columns we list whether LIMS, MR-SNe, and MNS channels are active or not, respectively. We point out that in the case of model ‘R-150 MNS’ MNS are assumed to merge with a short and constant time delay of 10 Myr instead that with a DTD.

Model	v_{MS} (km s $^{-1}$)	LIMS	MR-SNe	MNS
R-0	0	✓	✓	✓
R-150	150	✓	✓	✓
R-300	300	✓	✓	✓
R-150 MNS	150	✓	X	✓
R-150 MRD	150	✓	✓	X
noR-0	0	✓	X	X
noR-150	150	✓	X	X
noR-300	300	✓	X	X

5 RESULTS

Before discussing the comparison between our model predictions and the relevant observations for neutron-capture elements, we show the evolution of some important quantities as functions of time.

In the upper panel of Fig. 1, we report the time evolution of the SFR as predicted by our model at different Galactocentric radii. In contrast with Grisoni et al. (2018), the SFR during the thick disc phase is not the same for every Galactocentric distance up to 18 kpc, since we do not assume a constant thick disc mass density, but rather an exponentially decaying surface density profile, as described in Palla et al. (2020). As in the previously mentioned works, even without assuming a threshold for the star formation (SF), we are still able to obtain a quenching in the SF between the thick and the thin disc phases. The observed SFR in the solar neighbourhood (see Guesten & Mezger 1982; Prantzos et al. 2018 (hereafter P18)) is well reproduced by our model, as shown in the zoomed plot.

In the lower panel of Fig. 1, we report our predictions for the rates of SNeIa, SNeII, and MNS, averaged over the whole disc. The observational data are taken from Cappellaro et al. (1999) for SNeIa and SNeII. For MNS, we consider the latest cosmic rate observed by Abbott et al. (2021), i.e. 320_{-240}^{+490} Gpc $^{-3}$ yr $^{-1}$. We then applied the same conversion procedure developed by Simonetti et al. (2019) in order to convert the cosmic rate into a Galactic one. The rate so obtained is $R_{\text{MNS}} = 32_{-24}^{+49}$ Myr $^{-1}$, in agreement within the error bars with the rate of Kalogera et al. (2004), derived from binary pulsars.

5.1 Abundance ratios versus metallicity trends

In the next sections, we will show results for the evolution of the [Eu/Fe] versus [Fe/H] abundance patterns of the neutron-capture elements studied in this work. First, we will discuss results for Eu, a pure r-process element, and then for the other s-process and mixed-r-process elements.

5.1.1 Europium

In Fig. 2, we report the [Eu/Fe] versus [Fe/H] abundance pattern traced by the observational data (field stars and OCs) and compare it to the predictions of our models. As reported by Van der Swaelmen et al. (2023), who investigated the same Eu data, only for metallicity lower than ~ -0.8 dex it is possible to distinguish the famous Eu plateau at [Eu/Fe] ~ 0.4 dex for the field stars sample. Moreover, the plateau is visible more clearly only for stars belonging to the inner disc ($R_{\text{GC}} < 7$ kpc). For inner-disc stars, a scatter of ~ 1 dex

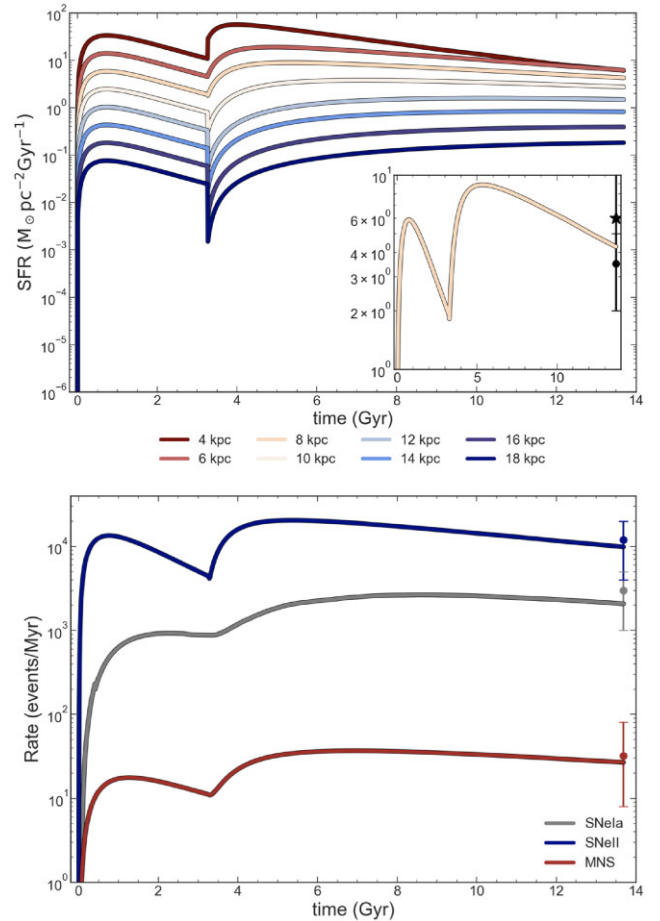


Figure 1. Upper panel: Time evolution of the SFR as predicted by our models at various Galactocentric distances. Right corner plot: Predicted SFR in the solar neighbourhood compared with present-day estimates (Guesten & Mezger 1982; P18). Lower panel: Predicted SNeIa, SNeII, and MNS rates compared with present-day observations from Cappellaro, Evans & Turatto (1999; for SNe) and estimate from Abbott et al. (2021; for MNS).

is present below [Fe/H] ~ -1.8 . However, this is due most probably to measurement errors rather than the stochastic enrichment of Eu characteristic of the halo (see Cescutti & Chiappini 2014; Cescutti et al. 2015; Wanajo, Hirai & Prantzos 2021). On the other hand, the field stars sample does not extend below [Fe/H] = -1.2 (-0.5) dex for $7 < R_{\text{GC}}/\text{kpc} < 9$ ($R_{\text{GC}} > 9$ kpc). The OC sample well overlaps with the field one for all R_{GC} and it is affected by a lower scatter, especially in the inner-disc region.

Fig. 2 shows results of model R-150 computed at $R_{\text{GC}} = 12$ kpc, $R_{\text{GC}} = 8$ kpc, and $R_{\text{GC}} = 6$ kpc compared with outer-, local-, and inner-disc data, respectively. No difference is expected if the rotational velocity of massive stars is changed, since in our model rotation does not affect Eu production. The curves are colour coded by the age of the stars created by the chemical evolution code. At age $\simeq 10.44$ Gyr, we notice the characteristic loop feature of the model due to the second infall phase. The accretion of pristine gas has the effect of decreasing the metallicity while having little impact on the [Eu/Fe] ratio. When the SF resumes, a rise in the [Eu/Fe] ratio is produced, then the ratio decreases while [Fe/H] increases because of the enrichment from SNeIa (see also Spitoni et al. 2019, 2020; Palla 2021). The model tends to overestimate the age of the clusters in the outer zone, since the OCs have age $\lesssim 7$ Gyr. However, the

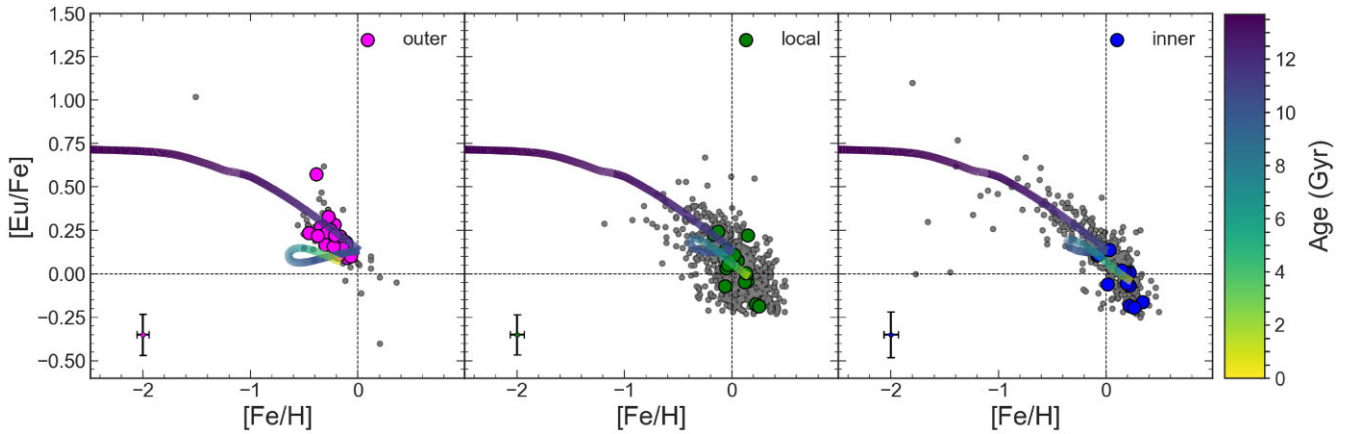


Figure 2. Predicted $[\text{Eu}/\text{Fe}]$ versus $[\text{Fe}/\text{H}]$ abundance patterns for the outer ($R_{\text{GC}} = 12$ kpc), local ($R_{\text{GC}} = 8$ kpc), and inner disc ($R_{\text{GC}} = 6$ kpc). The curves refer to the predictions of model R-150 (see Table 1) and are colour coded by the age of the stars created by the chemical evolution code. The grey small dots refer to the sample of field stars.

observed $[\text{Eu}/\text{Fe}]$ versus $[\text{Fe}/\text{H}]$ trend is overall well reproduced for all the three different regions. We fixed the percentage of MR-SNe in order to fit the main trend, rather than the solar value. In order to reproduce the solar abundance of Eu, a smaller percentage of MR-SNe progenitors should be assumed, of the order of 15 per cent. The local and the inner-disc curves slightly underestimate the metallicity reached by the observational data. This may be due to a too low SF efficiency and/or fraction of SNeIa systems. However, the model seems to reproduce rather well the SFR and SNIa rate at the present time in the solar neighbourhood (see Fig. 1). We also remind that in our model we do not include stellar migration effects which in principle can help reproducing the stars with larger $[\text{Fe}/\text{H}]$ values (see e.g. Spitoni et al. 2015; Palla et al. 2022). We confirm once again that the best scenario is the one in which both a quick source and a delayed one are responsible for the production of Eu. Here, the quick source is represented by MR-SNe and the delayed one by MNS with a DTD. This is not a novelty in chemical evolution simulations (e.g. Matteucci et al. 2014; Cescutti et al. 2015; Côté et al. 2019; Simonetti et al. 2019; Molero et al. 2021b). However, it must be noted that the quick source completely dominates the production of Eu. In fact, without the contribution from MNS, we would still be able to reproduce the observed abundance pattern. On the other hand, the $[\text{Eu}/\text{Fe}]$ versus $[\text{Fe}/\text{H}]$ pattern cannot be reproduced if MNS were the only producers of Eu, if a DTD is adopted. Only by assuming a constant and short time delay (~ 1 Myr) it is possible to explain the Eu enrichment as due to MNS alone (see Matteucci et al. 2014). Our model and prescriptions are slightly different from those adopted in Van der Swaelmen et al. (2023), but we confirm their same conclusion: Eu is produced mainly by a quick source and there is no need for an additional source at late times, at least in order to reproduce the observed Eu abundance pattern in the thin disc. However, it must be pointed out that MNS are the only source of heavy elements observed up to date, and because of that they cannot be excluded from chemical evolution simulations.

5.1.2 s-Process elements

The s-process elements studied in this work are: Ba, La, Zr, Y, and Ce. In Fig. 3, we report the observational data for both the field stars and the OC sets at each Galactocentric radius for $[\text{Y}/\text{Fe}]$ and $[\text{Ba}/\text{Fe}]$ versus $[\text{Fe}/\text{H}]$, taken as representative of the abundance pattern of s-process elements belonging to the first and second peak, respectively.

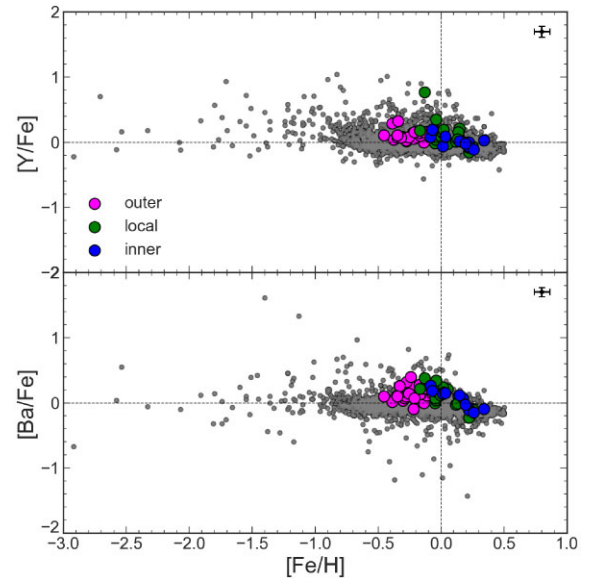


Figure 3. $[\text{Y}/\text{Fe}]$ and $[\text{Ba}/\text{Fe}]$ versus $[\text{Fe}/\text{H}]$ for our sample of field stars (in grey) and OCs (magenta, green, and blue dots) at all Galactocentric distances.

A characteristic s-process elements ‘banana’ shape is clearly seen at high metallicity, more pronounced in the $[\text{Ba}/\text{Fe}]$ than in the $[\text{Y}/\text{Fe}]$. This shape is assumed to reflect the pollution from LIMS during the AGB phase, which enrich the ISM with s-process material at later times creating the peak at $[\text{Fe}/\text{H}] \sim -0.04$ dex. The decrease for higher metallicity values is then due to Fe production from SNeIa. This pattern is visible both in the field and in OCs. In particular, the OCs belonging to the outer disc have lower $[\text{Fe}/\text{H}]$ and are characterized by an increasing pattern, the ones belonging to the solar region have nearly solar metallicity and display the peak followed by a slight decrease and finally the inner-disc OCs, which have the highest $[\text{Fe}/\text{H}]$, are characterized by a decreasing pattern, even if some of them overlaps with the trend defined by the solar-vicinity ones.

According to Prantzos et al. (2020), the fraction of the s-process elements studied in this work which is produced by the s-process is 78 per cent, 82 per cent, 89 per cent, 80 per cent, and 85 per cent for Y, Zr, Ba, La, and Ce, respectively, with the remaining fractions

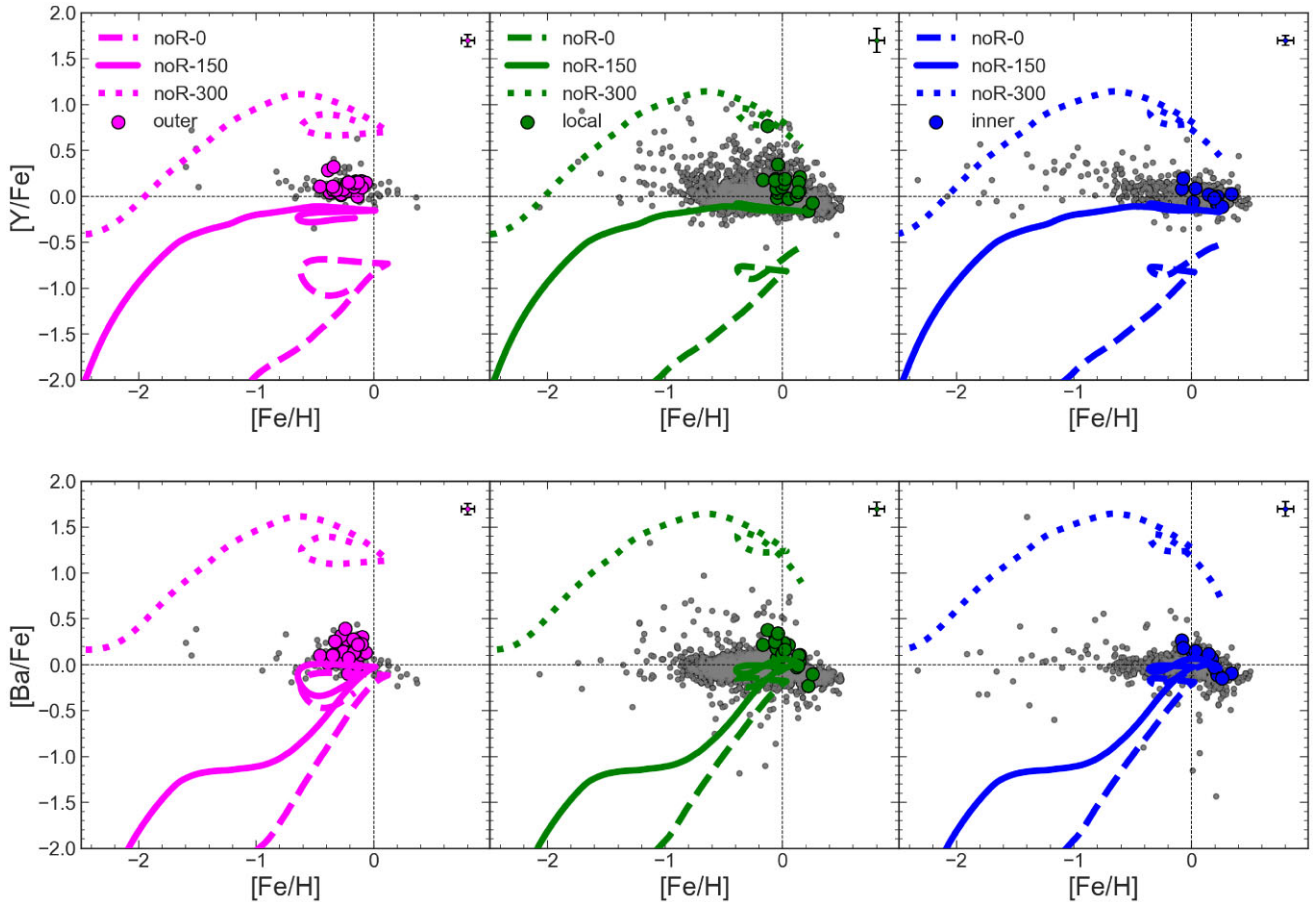


Figure 4. Predicted abundance patterns for $[Y/Fe]$ and $[Ba/Fe]$ versus $[Fe/H]$ for outer-disc ($R_{GC} = 12$ kpc), local-disc ($R_{GC} = 8$ kpc), and inner-disc ($R_{GC} = 6$ kpc) regions. We assume that only massive stars and LIMS are Y and Ba producers. The three lines in each plot correspond to different initial rotational velocities of massive stars (see legend and Table 1).

due mainly to the r-process (and in negligible or null amount to the p-process). Although the r-process fractions of those elements are not the predominant ones, we will show that from a chemical evolution point of view it is necessary to include it as well, in order to reproduce the observed abundance trends. Therefore, as a first step, we focus on the results of our model obtained when no r-process nucleosynthesis is taken into account by showing what happens when only rotating massive stars and LIMS contribute to the s-process elements production. Results of our model together with the observed abundance patterns for the s-process elements Y and Ba are reported in Fig. 4. Outer, local, and inner data are compared with our predicted evolution for $R_{GC} = 12$ kpc, $R_{GC} = 8$ kpc, and $R_{GC} = 6$ kpc, respectively. The three different curves refer to the three different initial rotational velocities for massive stars: 0, 150, and 300 km s^{-1} (see Table 1). The effect of rotation is clearly that of increasing the production of the s-process elements, especially for the elements belonging to the first s-process peak (Y in the figure), as expected. For the elements which belong to the second s-process peak (Ba in the figure), rotation must be increased to 300 km s^{-1} in order to see a significant enhancement in the stellar production. The second s-process production channel is represented by LIMS. With respect to previous chemical evolution studies, which adopted only yields from LIMS in the range of $1.5\text{--}3.0 M_{\odot}$, here we extend the mass range to $1.5\text{--}8.0 M_{\odot}$. We adopt yields from Cristallo et al. (2009, 2011, 2015) up to $6.0 M_{\odot}$ and yields obtained by extrapolation in the range

of $6.0\text{--}8.0 M_{\odot}$. Moreover, since those yields tend to overproduce the solar abundances of the s-process elements, we reduced them by a factor of 2, as suggested by R19 (see also Rizzuti et al. 2021).

In Fig. 5, we report the results of model R-150 for the evolution of all the s-process elements studied in this work with both the s- and the r-process astrophysical sites activated. We are showing only the model with massive stars with initial rotational velocities of 150 km s^{-1} since, once the contribution from MR-SNe is considered, the differences in the predicted abundance patterns between model assuming $v_{\text{rot}} = 0$ and 150 km s^{-1} are negligible and, as previously shown, models with $v_{\text{rot}} = 300 \text{ km s}^{-1}$ overestimate the observed abundance trends. The predicted curves are colour coded by the ages of the synthetic stars. We notice that the model is able to reproduce the main observed trends in the data, especially in the OC sample. The rise in the outer-disc data as well as the peak followed by the decrease in the local and inner-disc data are reproduced by our model at $R_{GC} = 12, 8,$ and 6 kpc. The only exceptions are represented by the $[Y/Fe]$ and the $[Zr/Fe]$ versus $[Fe/H]$ trends in the outer region for which the model does not produce the expected increase, but rather a decrease. This is probably due to the combination of too high MR-SNe yields and too low LIMS ones for those two elements. Because of the MR-SNe yields, the model predicts high $[Y/Fe]$ and $[Zr/Fe]$ value at relatively low metallicities and it is not able to produce an increasing trend at higher ones because LIMS are not producing enough Zr and Y abundances. However, it must be reminded that LIMS are

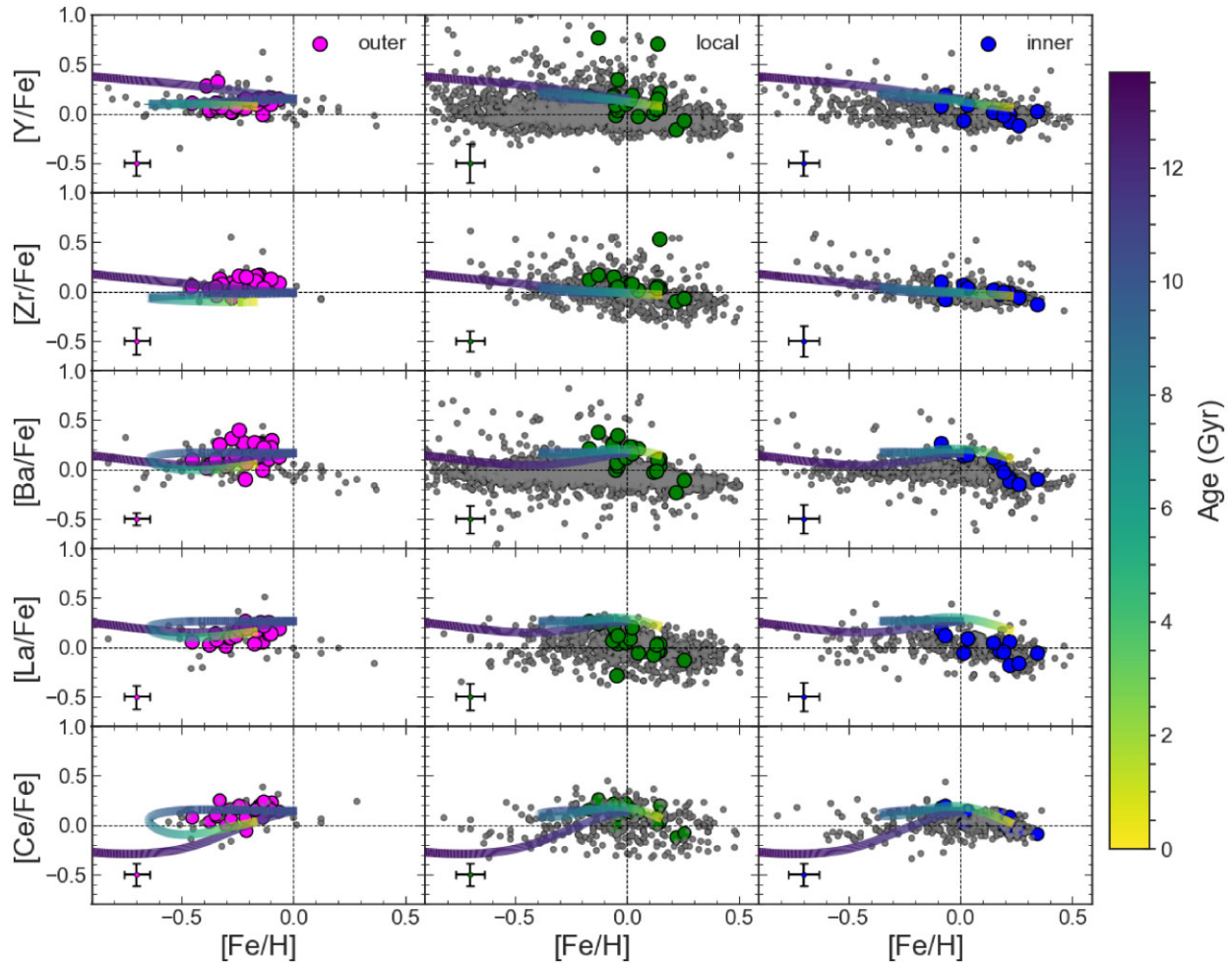


Figure 5. Predictions from model R-150 for the s-process elements abundance patterns versus $[\text{Fe}/\text{H}]$ for outer-disc ($R_{\text{GC}} = 12$ kpc), local-disc ($R_{\text{GC}} = 8$ kpc), and inner-disc ($R_{\text{GC}} = 6$ kpc) regions. The channels considered for the production of the s-process components are: massive stars with initial rotational velocities of 150 km s^{-1} and LIMS. The channels for the r-process components are: MR-SNe and MNS with a DTD. The curves are colour coded by the age of the stars created by the chemical evolution code.

not supposed to be among the main producers of Y and Zr, since those two elements belong to the first s-process peak. $[\text{La}/\text{Fe}]$ versus $[\text{Fe}/\text{H}]$ is slightly overproduced by the model in the local and inner-disc regions. The $[\text{Ce}/\text{Fe}]$ versus $[\text{Fe}/\text{H}]$ has recently been already studied by Contursi et al. (2023) in the MW halo and disc component through high-quality samples of GSP-Spec Ce abundances. They find a rather flat trend at a mean level of $[\text{Ce}/\text{Fe}] \sim 0.2$ dex for $-0.7 < [\text{M}/\text{H}] < 0.3$ dex which are able to reproduce by means of the three-infall chemical evolution model by Spitoni et al. (2023). On the other hand, our OC sample clearly shows the characteristic *banana* shape of s-process elements, rather than a flat trend, which is clearly well reproduced by our two-infall model. The three curves reach metallicities of $[\text{Fe}/\text{H}] \sim -0.16, 0.16,$ and 0.33 dex in the outer, local, and inner disc, respectively, which slightly underestimate the ones observed in the OC samples for the outer and local disc, similarly to what happen for Eu (see previous section).

5.1.3 Mixed-process elements

In Fig. 6, we report the observed abundance patterns for both field stars and OCs in our *Gaia*-ESO DR6 samples (see Section 2) together with the predictions from our model for Mo, Nd, and Pr. We refer to

those elements as mixed-process elements. In fact, even if for all the elements studied in this work both the contributions from the s- and the r-process have been considered; Mo, Nd, and Pr are found to owe a large fraction of their Galactic abundances to the r-process. As also discussed by Van der Swaelmen et al. (2023), different studies (e.g. Sneden, Cowan & Gallino 2008; Bisterzo et al. 2014; Prantzos et al. 2020) agree in assigning ~ 40 per cent of the r-process component to Nd and ~ 50 per cent to Pr. On the other hand, the contributions of the different processes to the abundance of Mo in the Sun differ from one author to another. According to Hansen, Andersen & Christlieb (2014), who presented a study of both Mo and Ru abundances in the MW covering both dwarfs and giants from $[\text{Fe}/\text{H}] \sim -0.7$ down to ~ -3.2 dex, Mo can be considered as a highly mixed element, with contributions from the main and weak s-processes as well as from the p-process and, in a smaller fraction, from the main r-process. In agreement with that study, more recently Prantzos et al. (2020) proposed for Mo a contribution of 50 per cent from s-process, 27 per cent from r-process, and 23 per cent from p-process. Van der Swaelmen et al. (2023), which adopted our same data set, examined also the origin of these elements from an observational point of view, comparing their abundance with that of Eu. From their study, it appears that Nd should be characterized by a significant s-process

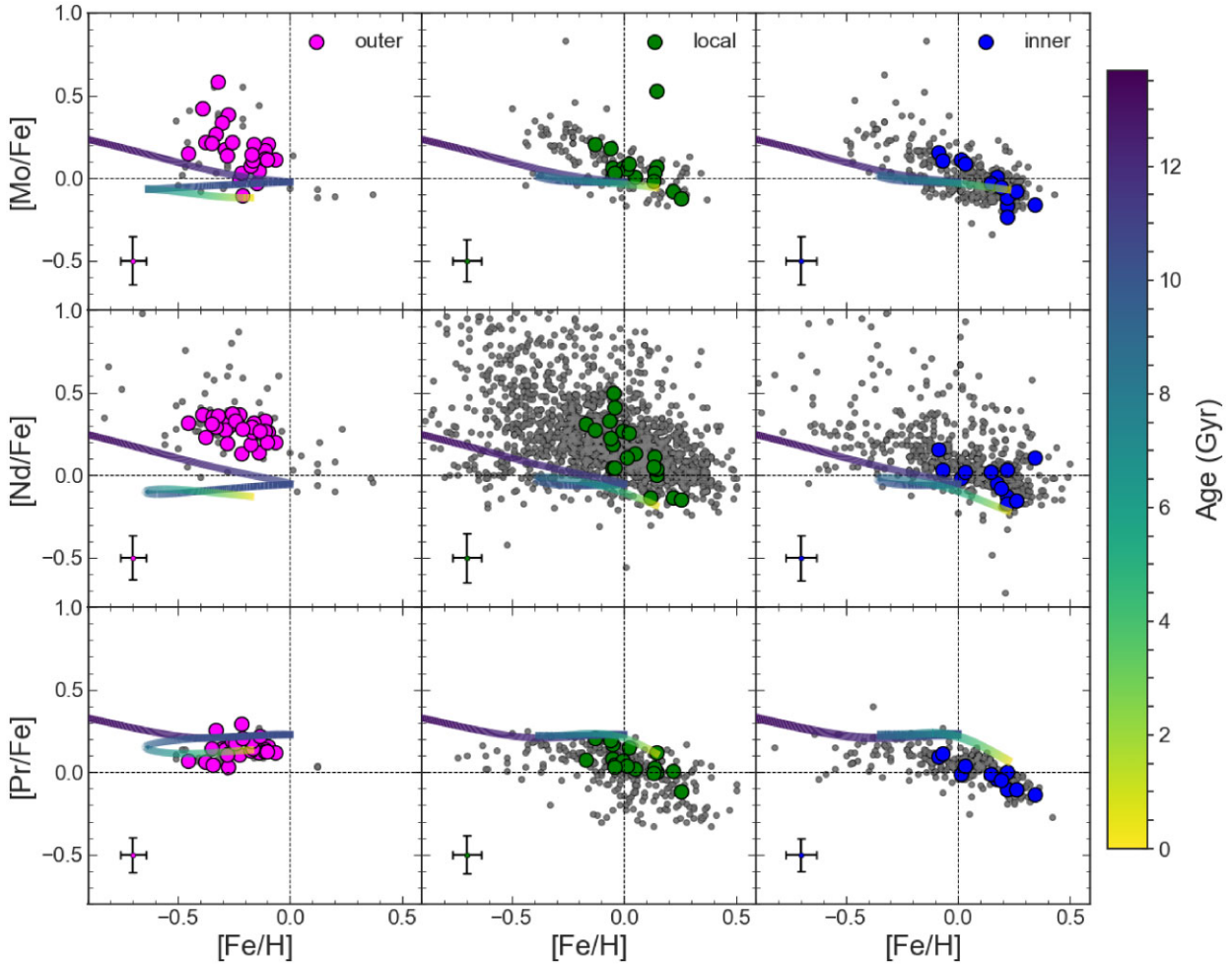


Figure 6. Predictions from model R-150 for the mixed-process elements abundance patterns versus $[\text{Fe}/\text{H}]$ for outer-disc ($R_{\text{GC}} = 12$ kpc), local-disc ($R_{\text{GC}} = 8$ kpc), and inner-disc ($R_{\text{GC}} = 6$ kpc) regions. The curves are colour coded by the age of stars created by the chemical evolution code.

contribution, whereas for Pr they expect a lower contribution from the s-process. Results of our model are not in agreement with these hypotheses for Nd and Pr. In fact, as shown in Fig. 6, our model predicts a too low $[\text{Nd}/\text{Fe}]$ versus $[\text{Fe}/\text{H}]$ abundance pattern with respect to the observed one. This discrepancy between predictions and observations may be attributed to LIMS which produce a too low amount of Nd with respect to what is expected in Van der Swaelmen et al. (2023). On the other hand, our model fits properly the $[\text{Pr}/\text{Fe}]$ versus $[\text{Fe}/\text{H}]$ trend, only slightly overproducing the observed pattern in the local and inner parts. This may be due both to a too strong production of Pr by massive stars and by LIMS, contrary to what happens for Nd. It is worth noting that the observed abundance pattern of $[\text{Pr}/\text{Fe}]$ versus $[\text{Fe}/\text{H}]$ resembles more that of an s-process element than the one of the $[\text{Nd}/\text{Fe}]$ versus $[\text{Fe}/\text{H}]$, at least when considering the *Gaia*-ESO OC data. In fact, in the case of Pr we distinguish a rise in the abundances in the outer region, followed by a peak and then a decrease in the local and inner regions. On the other hand, this typical ‘banana’ shape is not recognizable in the observed abundance pattern of Nd.

The behaviour of Mo is much more uncertain. As discussed in Van der Swaelmen et al. (2023), the elusive nature of this chemical element together with the difficulty in measuring its abundance caused chemical evolution studies to reach discordant conclusions about its cosmic origin. In Mishenina et al. (2019),

the $[\text{Mo}/\text{Fe}]$ versus $[\text{Fe}/\text{H}]$ abundance pattern has been studied in a wider range of metallicities with respect to our samples and with chemical evolution models from Travaglio et al. (2004) and P18 and with the open-source galactic chemical evolution code OMEGA + (Côté & Ritter 2018). Their main conclusion is that canonical stellar sources of heavy elements are not producing a sufficient amount of Mo to reproduce observations. They showed that, despite the fact that the r-process contributes to a small fraction of the solar Mo, it is of significant importance especially at low metallicities, where the s-process contribution from AGB stars is negligible. In fact, in Mishenina et al. (2019), the model that better agrees with the data is the one in which the r-process component of Mo is produced on quick time-scales (the r-process production site considered is associated with MNS with a short and constant delay time for merging). Our results for the $[\text{Mo}/\text{Fe}]$ versus $[\text{Fe}/\text{H}]$ abundance pattern are in agreement with Mishenina et al. (2019) conclusions. In fact, even with a quick r-process source activated (in our case represented by MR-SNe) the predicted trends appear to slightly underestimate the observed ones at each Galactocentric radius. However, this is most probably due to the lack in our model of an additional contribution from neutrino-driven SNe which may be important producers of Mo at all metallicities (see e.g. Bliss, Arcones & Qian 2018; Bliss et al. 2020).

5.1.4 Comparison with previous studies

Similar prescription to those adopted in this work have been already included in chemical evolution studies by P18 and R19 in order to study the contribution from rotating massive stars to the enrichment of different chemical species in the MW. The main differences between the work of R19 and this one are: (i) the set of Limongi & Chieffi (2018) for rotating massive stars used by R19 is the Set F whereas we adopt Limongi & Chieffi (2018)'s recommended Set R (see also Romano et al. 2019); (ii) in R19, LIMS in the 1.3–3.0 M_{\odot} mass range are assumed to produce s-process elements, whereas we extend the mass range to 1.3–8.0 M_{\odot} ; (iii) for the r-process nucleosynthesis we use both MR-SNe and MNS, with these latter characterized by having a DTD, while R19 used either one source or the other (with the coalescence time-scale for MNS constant and equal to 1 Myr); and (iv) the iron yields from CC-SNe adopted in R19 are those from Kobayashi et al. (2006), while for consistency here we adopt the ones from Limongi & Chieffi (2018). On the other hand, the main differences between the work of P18 and our are: (i) in P18, r-process elements are assumed to be produced in CC-SNe and their yields are scaled to the yield of oxygen according to the Solar system r-process contribution as determined by Sneden et al. (2008); the yields so obtained, are functions of the mass and of the metallicity of the star and (ii) the yields of rotating massive stars are weighted with a metallicity-dependent function empirically determined.

The main difference between our results and those of R19 is that in their model it appears that the contribution from MR-SNe is not the dominant one at really low metallicities. In fact, it is still possible to appreciate differences between their model in which massive stars have an initial rotational velocity of 150 km s^{-1} and the one in which massive stars do not rotate at all, even when the MR-SNe channel is active (their models LC000+MRD and LC150+MRD). These differences are visible only at really low metallicities (< -4 dex). For higher [Fe/H] the two models are very similar, exactly as it happens in our case. So that, for the metallicities we are interested in this work, we do not expect significant differences. The dissimilarities in the prescriptions adopted for MR-SNe nucleosynthesis between our work and that of R19 may be responsible for the slightly different results between the two studies.

The discrepancies between our predictions and those of P18 are not so strong, even if their prescription for the production of heavy elements from massive stars is substantially different from ours. In fact, they assume that all CC-SNe can produce heavy elements and scale their yields to the one of oxygen, whereas in our case only a small fraction of massive stars can produce r/s- process material with the nucleosynthesis of Nishimura et al. (2017). The major issue which results from our approach is that the adopted yields are not a function of the metallicity and, in particular, of the mass of the progenitor. That means that all the assumed 20 per cent of stars with progenitor mass of 10–25 M_{\odot} are producing the same amount of r-process material independently from the metallicity, which is of course an oversimplification. P18 assumed that the yield of each heavy element considered scales with another element produced exclusively by massive stars which reproduce the solar abundance, with this latter being already a function of mass and metallicity. This method still has some uncertainties but it can be reliable for the purpose of P18, which is the study of the effect of rotating massive stars yields. In our case, the primary goal is that of studying the origin of neutron-capture elements by adopting the state-of-the-art in the nucleosynthesis prescriptions and, as a result, to reveal the main uncertainties in both the chemical evolution models and the nucleosynthesis itself.

5.2 Gradients

Here, we present the abundance gradients of the studied elements. We first show our predictions for the present time abundance gradients along the disc and then discuss their time evolution.

5.2.1 Present-day radial abundance gradients

In Fig. 7, we compare the theoretical present-day gradients of [Fe/H] and [Eu/H] to the observational data. In order to compare present-day results of our model with the observations, we restricted our OC sample to clusters with age ≤ 3 Gyr. As discussed in M23 (see also references therein) there is a general agreement about the existence of a steeper [Fe/H] gradient in the inner disc and an extended plateau in the outer region, with a cutoff point at $R_{GC} \sim 11.2$ kpc. This change of slope is evident in the OC sample used in this work and it is still visible when we restrict our sample to OCs younger than 3 Gyr. Considering the entire OC sample and a weighted single-slope fit, M23 find a slope of the [Fe/H] gradient of -0.054 ± 0.004 dex kpc^{-1} . Considering the two radial regions they obtain a steeper inner gradient (-0.081 ± 0.008 dex kpc^{-1}) and a much flatter outer plateau (-0.044 ± 0.014 dex kpc^{-1}). The slopes of the restricted OC sample are in good agreement with the ones of the whole sample, as reported in Table 2. The slope of the [Fe/H] gradient predicted by our model is equal to -0.067 ± 0.003 dex kpc^{-1} . As shown in Fig. 7, this is slightly steeper both with respect to the gradients of the restricted OC sample (upper panel) and to the one of the Cepheid sample including the data of Luck & Lambert (2011) and Genovali et al. (2015) (lower panel). However, our result is in good agreement with other recent literature slopes of the [Fe/H] gradient from OC samples (Carrera et al. 2019; Donor et al. 2020; Spina et al. 2021; Zhang, Chen & Zhao 2021; Spina, Magrini & Cunha 2022, see table 1 in M23).

In the right-hand panels of Fig. 7, we compare the slopes predicted by our model under different assumptions (see Table 1) for the [Eu/H] gradient with those observed in the restricted OC sample and in the Cepheid one from Luck & Lambert (2011). The OC restricted sample shows a flat [Eu/H] gradient, with a global slope equal to -0.017 ± 0.004 dex kpc^{-1} and an inner slope slightly steeper than the outer one (see Table 2). In general, elements which are produced on longer time-scales are characterized by steeper gradients than elements produced on fast time-scales. For example, α -elements have flatter slopes than Fe-peak elements (even if there may be differences also between elements of the same group). Therefore, the shape of the [Eu/H] gradient points towards a short time-scale of production. We remind that in model R-150 (variable ν) the r-process material comes from both a quick source (MR-SNe) and a delayed one (MNS with a DTD). In Fig. 7, this model is represented by the olive line. It predicts a global slope equal to -0.051 ± 0.003 dex kpc^{-1} , which is too steep with respect to the one observed from the OC sample. The agreement with the data does not improve even if we assume that Eu is produced only on short time-scales [purple and teal lines in the figure, corresponding to Eu production from solely MR-SNe and MNS with a constant and short (10 Myr) delay time for merging, respectively]. Moreover, these two models predict the same slope of the [Eu/H] gradient, equal to -0.049 ± 0.003 dex kpc^{-1} . Our results do not improve noticeably even if the contribution from the delayed source is suppressed, because MNS with DTD are not the main source of r-process material in model R-150. In fact, even if their Eu yield is higher with respect to that of MR-SNe, their rate is low (see Fig. 1). We stress once again that MNS are the only source of r-process material confirmed by observations and therefore they

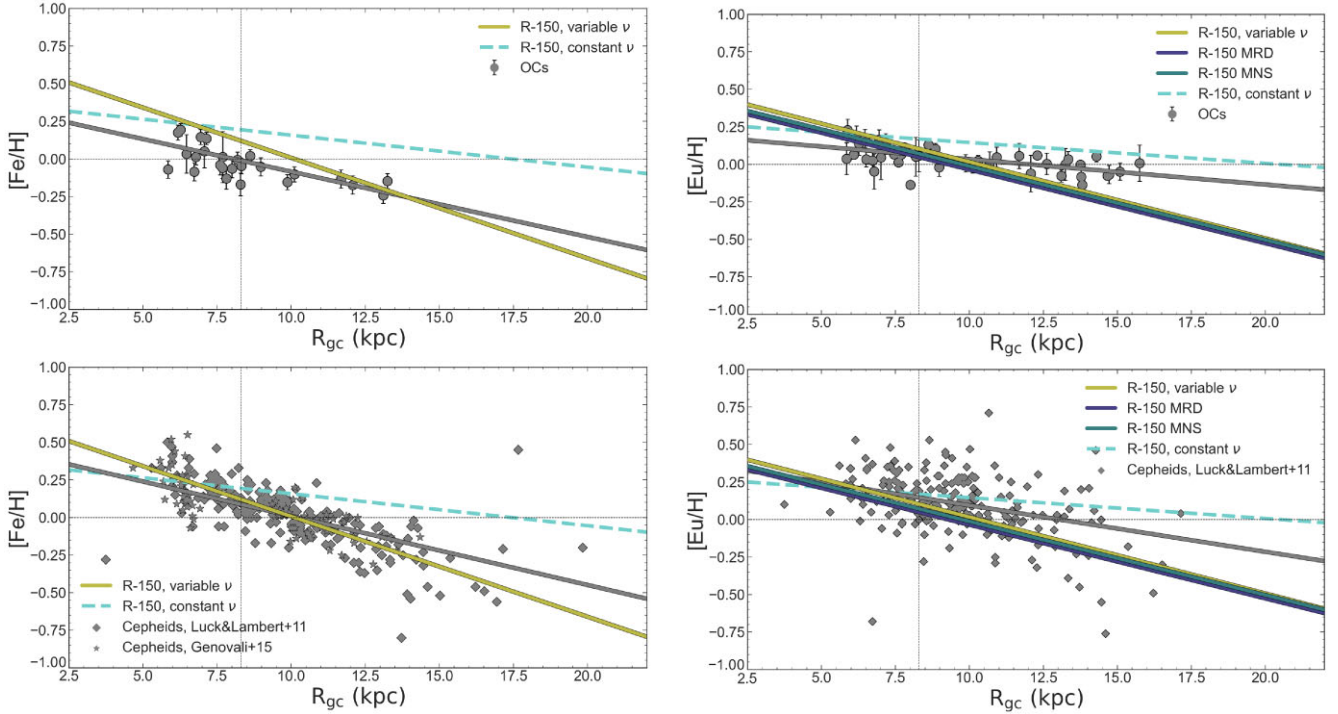


Figure 7. Prediction of the present-day slope of the $[\text{Fe}/\text{H}]$ and $[\text{Eu}/\text{H}]$ gradients from our models with variable (olive line) and constant (dashed turquoise line) SF efficiency compared with the one of the restricted (age ≤ 3 Gyr) OC sample (upper panel) and the Cepheid sample (lower panel) with data from Luck & Lambert (2011) (grey diamonds) and Genovali et al. (2015) (grey stars). For the $[\text{Eu}/\text{H}]$, we show also models with Eu produced only by MR-SNe (purple line) and Eu produced only by MNS with a constant and short delay time for merging (teal line). The grey lines represent the linear fit of the observational data.

Table 2. Slopes of the $[\text{Fe}/\text{H}]$ and $[\text{Eu}/\text{H}]$ gradients of the reduced (Age ≤ 3 Gyr) OC sample and as predicted by our model for the all, inner ($R_{\text{GC}} < 11.2$ kpc) and outer ($R_{\text{GC}} > 11.2$ kpc) radial region. For comparison we show also the one obtained from the Cepheid sample of Luck & Lambert (2011) and Genovali et al. (2015). In the case of Eu we show predictions also of models in which Eu is produced either by MR-SNe or by MNS with a constant and short delay time for merging.

	$[\text{Fe}/\text{H}]$			$[\text{Eu}/\text{H}]$		
	m_{tot} (dex kpc $^{-1}$)	m_{inner} (dex kpc $^{-1}$)	m_{outer} (dex kpc $^{-1}$)	m_{tot} (dex kpc $^{-1}$)	m_{inner} (dex kpc $^{-1}$)	m_{outer} (dex kpc $^{-1}$)
OCs	-0.049 ± 0.005	-0.081 ± 0.013	-0.045 ± 0.017	-0.017 ± 0.003	-0.024 ± 0.009	-0.015 ± 0.014
Cepheids	-0.046 ± 0.003	–	–	-0.031 ± 0.004	–	–
Model R-150 var ν	-0.067 ± 0.002	-0.064 ± 0.008	-0.063 ± 0.007	-0.051 ± 0.003	-0.038 ± 0.004	-0.057 ± 0.007
Model R-150 con ν	-0.021 ± 0.004	-0.044 ± 0.008	-0.007 ± 0.001	-0.014 ± 0.003	-0.029 ± 0.006	-0.004 ± 0.001
Model R-150 MRD	–	–	–	-0.049 ± 0.003	-0.034 ± 0.003	-0.057 ± 0.007
Model R-150 MNS	–	–	–	-0.049 ± 0.003	-0.034 ± 0.003	-0.057 ± 0.007

must be included in the computation. However, when compared with the MR-SNe, they are not the dominant source. On the other hand, by including them the agreement between our predicted $[\text{Eu}/\text{H}]$ inner slope and the observed one improves, especially for models with no delayed source (see Table 2).

To reproduce flatter present-day abundances gradients we tested also a model with constant SF efficiency ($\nu = 1$ Gyr $^{-1}$). Results for the $[\text{Fe}/\text{H}]$ and for the $[\text{Eu}/\text{H}]$ are reported in Fig. 7 as well as in Table 2. By assuming a constant SF efficiency we obtain a satisfactory agreement with the OCs $[\text{Eu}/\text{H}]$ gradient. On the other hand, we lose the agreement with the observed $[\text{Fe}/\text{H}]$ gradient, in particular in the outer regions where the predicted SF turns out to be too intense. As already pointed out by Grisoni et al. (2018), the inside-out scenario, although is a key ingredient for the formation of the Galactic discs, is not enough to explain the abundance pattern at different Galactocentric distances and the abundance gradients by

itself. Models with only an inside-out scenario usually predict too flat present-day gradients, as is the case of our model with constant SF efficiency. In order to steepen the gradients further assumptions are needed. In particular, one needs to consider either a variable SF efficiency or radial gas flows or a combination of both (Palla et al. 2020). Models with decreasing SF efficiency with increasing Galactic radius produce a steeper gradient, since they boost the chemical enrichment in the inner regions relative to the outer ones. Radial migration of stars, which is not taken into account in any of our models, on the contrary, should have the effect of flattening the gradient on long enough time-scales (Minchev et al. 2018; Quillen et al. 2018). Whether clusters are affected by migration as much as field stars is not completely understood yet. If also clusters with age < 3 Gyr are affected by migration, the discrepancy between our models and the data (especially in the outer region) may be partially due to the moving outward of ‘old’ clusters formed in the inner disc

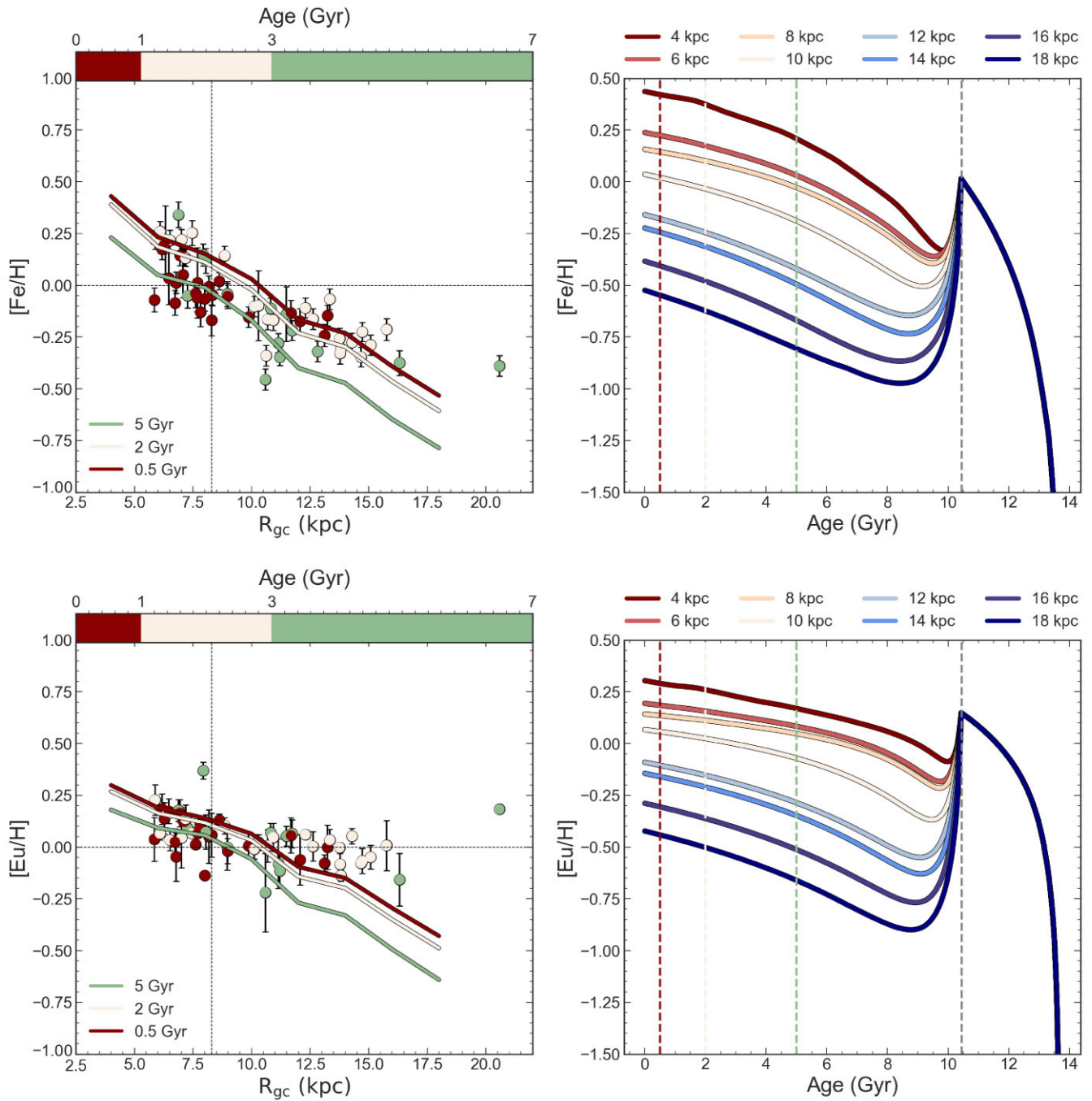


Figure 8. Left-hand panels: Time evolution of the radial [Fe/H] and [Eu/H] gradients as predicted by model R-150. The OC sample is divided in three age bins: young (age < 1 Gyr), intermediate (1 < age < 3 Gyr), and old (age > 3 Gyr). Solid lines are the results for the [Fe/H] gradient as predicted by our model at 0.5, 2, and 5 Gyr. Right-hand panel: Time evolution of the [Fe/H] and [Eu/H] as predicted by model R-150 for different Galactocentric distances. Vertical dotted lines indicate the ages considered to compute the gradients.

(see M23 and references therein). In favour of this hypothesis, the slopes of the [Eu/H] gradient predicted by our models with variable SF efficiency are in better agreement with the one computed from the younger Cepheid sample of Luck & Lambert (2011), shown in the lower panels of Fig. 7 (see Table 2).

5.2.2 Time evolution of the radial abundance gradients

In the upper left panel of Fig. 8, we report the time evolution of the radial [Fe/H] gradients of the completed OC sample divided in three

age bins together with results of our model at 0.5, 2, and 5 Gyr. In the upper right panel of the same figure, we report the predictions about [Fe/H] evolution as a function of age for different radii. The drop at age ~ 10.44 Gyr, in correspondence of the vertical grey dotted line, is the effect of the dilution event which happens when the second infall forming the thin disc takes place. Since we are comparing our results with OCs in the thin disc, we are interested only in the evolution from age ~ 10.55 Gyr until the present day.

As observed by M23, the youngest clusters of the sample (age < 1 Gyr) have lower metallicity than the older ones in the inner disc

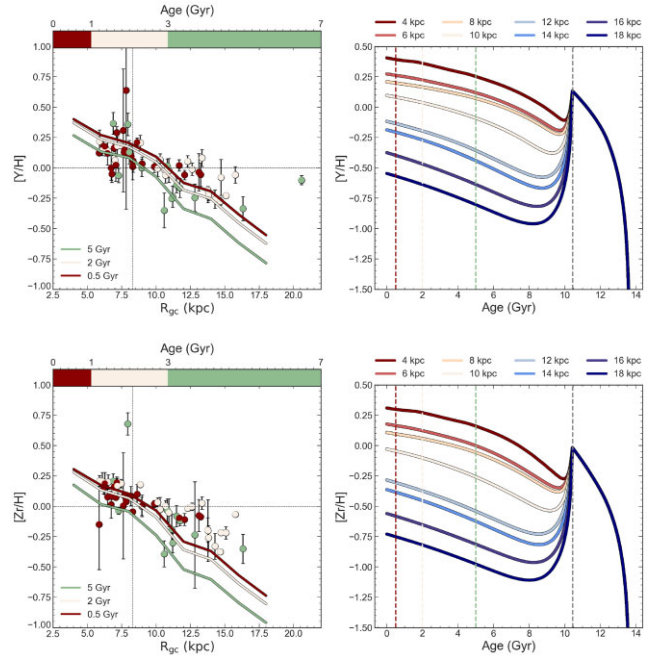
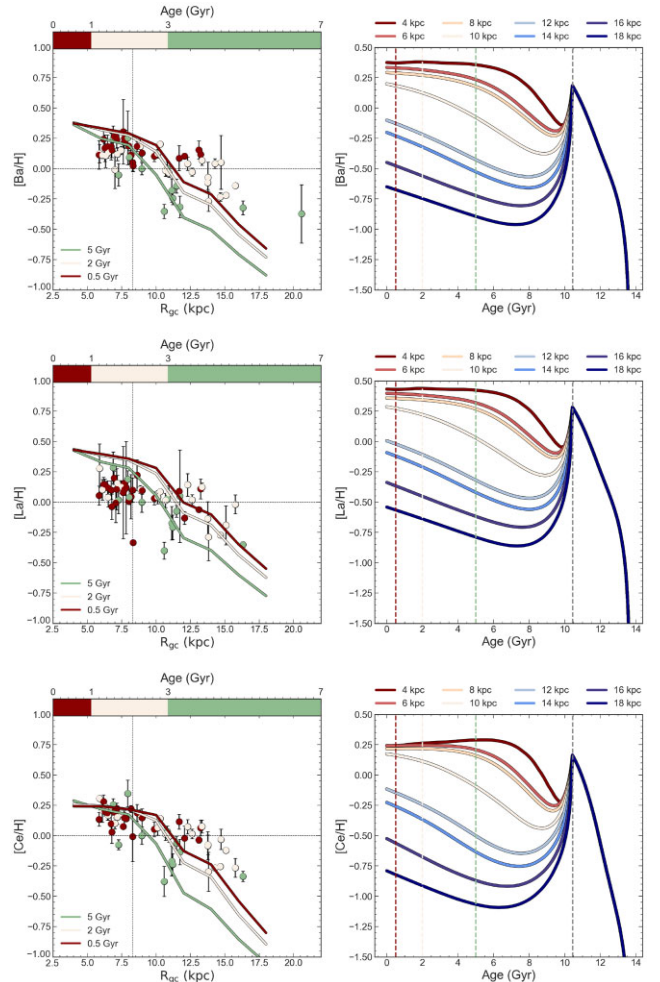
Table 3. Slopes of the [E/H] gradients predicted by our model at age = 0.5, 2, and 5 Gyr.

	Age = 0.5 Gyr	Age = 2 Gyr	Age = 5 Gyr
[Fe/H]	-0.067 ± 0.002	-0.069 ± 0.002	-0.073 ± 0.003
[Eu/H]	-0.051 ± 0.003	-0.053 ± 0.004	-0.059 ± 0.004
[Y/H]	-0.067 ± 0.004	-0.070 ± 0.004	-0.077 ± 0.005
[Zr/H]	-0.075 ± 0.004	-0.078 ± 0.004	-0.083 ± 0.004
[Ba/H]	-0.078 ± 0.008	-0.084 ± 0.007	-0.095 ± 0.006
[La/H]	-0.073 ± 0.008	-0.080 ± 0.007	-0.092 ± 0.006
[Ce/H]	-0.077 ± 0.011	-0.087 ± 0.011	-0.105 ± 0.008
[Mo/H]	-0.071 ± 0.003	-0.073 ± 0.003	-0.077 ± 0.004
[Pr/H]	-0.078 ± 0.012	-0.089 ± 0.012	-0.109 ± 0.009
[Nd/H]	-0.058 ± 0.004	-0.062 ± 0.004	-0.070 ± 0.005

($R_{GC} < 10$ kpc). As expected, the trend in the youngest clusters is not in agreement with our chemical evolution simulations which predict that the oldest population should be less enriched than the youngest one (on the other hand, an additional recent third infall episode produces a chemical impoverishment of the young population; see Spitoni et al. 2023). The young clusters also show a flatter [Fe/H] gradient with a slope of -0.038 ± 0.004 (for age < 1 Gyr), -0.063 ± 0.006 (for $1 \leq \text{age} \leq 3$ Gyr), and -0.084 ± 0.019 (for age > 3 Gyr) (see table A.10 of M23). The slopes predicted by our model at 5, 2, and 0.5 Gyr reproduce this trend, but the difference between the three slopes is not that significant (see Table 3). Larger variations with time of the gradient slopes would be obtained by comparing our model results at older times. On the other hand, really small changes are expected in the latest Gyrs, as it appears clear from the upper right panel of Fig. 8. According to M23, the observed trend in the youngest clusters is most likely due to a bias introduced by the standard spectroscopic analysis of low-gravity giant stars. If the gradient of the youngest population is recomputed by removing giant stars with $\log g < 2.5$ the final gradient is very close to that of OCs with $1 < \text{age} < 3$ Gyr which suggests a limited time evolution of the gradient, in agreement with our models.

The lower panels of Fig. 8 are the same as the upper panels, but for Eu. Here, we show results of our model R-150. Unlike [Fe/H], in the case of Eu, the OC sample gradient does not show different shapes with time. The youngest population shows abundances consistent with that of the intermediate and older clusters. Our model is in agreement with this trend, in fact it predicts very similar slopes for the three different lines corresponding to ages of 0.5, 2, and 5 Gyr (see Table 3). As already discussed previously, we predict a steeper present-day slope with respect to the observed one. This is true also for the different ages shown in Fig. 8. However, as for the present-day gradients, also at different ages, we obtain a much better agreement with the data of the inner ($R_{GC} < 11.5$ kpc) disc rather than with those of the outer parts, where our model struggles to reproduce the observed plateau. This could be due to the too low SF efficiencies assumed for the outer part of the disc. However, it must be pointed out that we do not expect much higher SF in the outer disc and the SF efficiency has been fine-tuned to reproduce the abundance patterns of the OCs with $R_{GC} > 9$ kpc, as shown in the previous sections. Higher values of the SF efficiency would produce a too high metallicity and the agreement with both the abundances pattern and the [Fe/H] gradients would be lost.

In Figs 9 and 10, we display the time evolution of the first and second peak s-process elements, respectively. In this case, the OC sample shows much more scatter. According to M23, the OC sample is characterized by an inverse main trend with respect to [Fe/H], with the youngest clusters being characterized by lower (or almost equal)

**Figure 9.** Same as Fig. 8 but for 1st peak s-process elements.**Figure 10.** Same as Fig. 8 but for 2nd peak s-process elements.

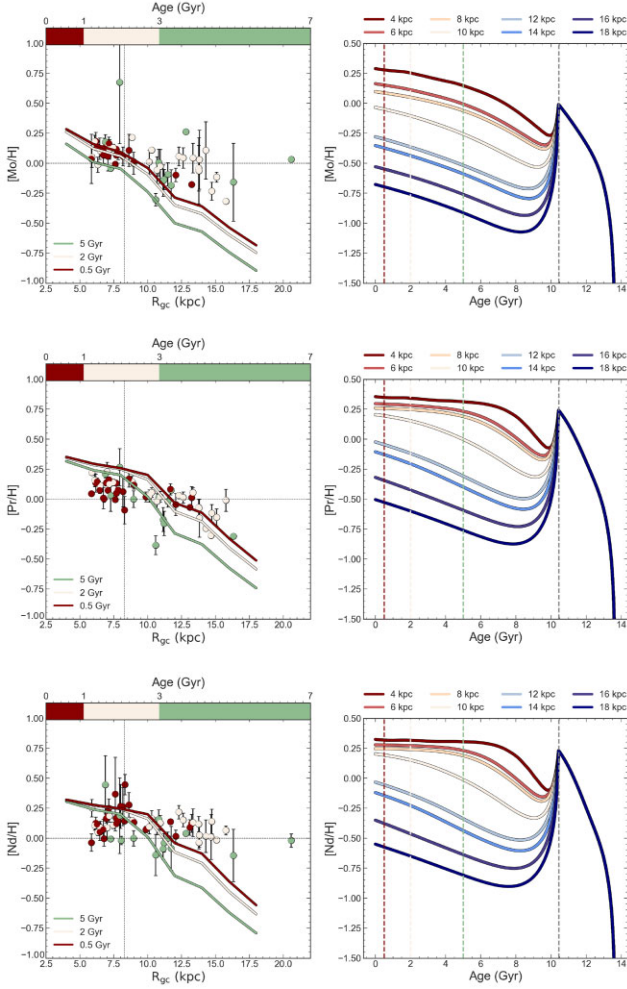


Figure 11. Same as Fig. 8 but for mixed-process elements.

abundances of Y, Zr, Ba, La, and Ce than their older counterparts. Predictions of our model are in agreement with these trends. For Y and Zr, the lines corresponding to ages of 0.5 and 2 Gyr show a very similar pattern and are characterized by both the same slope and almost the same abundances at all Galactocentric distances. Similarly, in the case of Ba, La, and Ce, our model predicts an almost identical flat or slightly decreasing pattern at all ages in the inner zones ($R_{GC} < 10$ kpc), while the predictions diverge for higher R_{GC} values. The plateau observed for the s-process elements belonging to the second peak at low Galactocentric distances, is due to the effect of LIMS, which contribution reaches a maximum value faster in the inner regions than in the outer ones (see also Casali et al. 2023). The slopes predicted by our model for the first peak s-process elements are globally flatter with respect to those expected for the second peak elements. This is because Y and Zr are mainly produced by rotating massive stars (Limongi & Chieffi 2018) and therefore on quicker time-scales with respect to Ba, La, and Ce which, on the other hand, have a production dominated by LIMS (Cristallo et al. 2009, 2011, 2015).

The time evolution of the gradients of the other r-/mixed-process elements is reported in Fig. 11. The OC sample shows a slope similar to that of Eu (~ -0.002 dex kpc^{-1} , see M23), but, as in the case of the s-process elements, also the mixed-/r-process elements are characterized by a larger scatter, in particular Mo and Nd. Unlike the

[Fe/H] gradient, in the case of those elements the youngest population does not appear to be more abundant than the oldest one. As already discussed in Section 5.1.3, because of the specific nucleosynthesis prescriptions adopted in this study our model underestimates the observed Mo and Nd abundances. It is possible to note that a similar plateau in the inner region predicted by our model for the s-process elements belonging to the second peak appears also for Nd and Pr. Once again, this may be due to the contribution from LIMS which reaches its maximum value faster in the inner regions.

6 SUMMARY AND CONCLUSIONS

In this paper, we studied the origin of neutron-capture elements in the MW by taking advantage of the large sample of OCs from the *Gaia*-ESO DR6. To this aim, we adopted the revised two-infall model (Palla et al. 2020, see also Spitoni et al. 2019). We investigated the abundance patterns and the radial gradients of five s-process (Y, Zr, Ba, La, and Ce) and four mixed-/r-process elements (Eu, Mo, Nd, and Pr). In order to do that, we adopted the following nucleosynthesis prescriptions: s-process material is produced by (i) rotating massive stars ($M > 13 M_{\odot}$) with yields from Limongi & Chieffi (2018) with three different initial rotational velocities (0, 150, and 300 km s^{-1}) and by (ii) LIMS ($1 \leq M/M_{\odot} \leq 8$) with yields from the FRUITY data base (Cristallo et al. 2009, 2011, 2015) in the 1–6 M_{\odot} range, arbitrarily extrapolated up to 8 M_{\odot} . R-process material is produced by both a prompt and a delayed source, namely (i) MR-SNe which are supposed to be 20 per cent of all massive stars with initial mass between 10 and 25 M_{\odot} with yields from Nishimura et al. (2017) (model L0.75) and (ii) MNS with a DTD from Simonetti et al. (2019) with $\beta = -0.9$ with yields prescriptions from Molero et al. (2021b) best model. Our conclusions for the abundances patterns of [E]/[Fe] versus [Fe/H] can be summarized as follows:

(i) The [Eu/Fe] versus [Fe/H] abundance pattern is well reproduced if both a quick source and a delayed one act as r-process producers. This is a well-known result in chemical evolution. However, here we stress how with the assumed prescriptions the quick source completely dominates the production of Eu, in agreement with the recent work of Van der Swaelmen et al. (2023) according to which there is no need for an additional delayed source at least to reproduce the abundance pattern in the thin disc. However, since MNS are the only observed source of neutron-capture elements up to now, they cannot be excluded from chemical evolution models computations.

(ii) The s-process elements' abundances pattern is not reproduced if one considers only production from typical s-process astrophysical sources as rotating massive stars and LIMS. Rotation increases the production of s-process material, especially at low metallicities and for elements belonging to the first s-process peak, but the r-process component must also be taken into account.

(iii) When the contribution from MNS and MR-SNe to the production of the r-process component of the s-process elements is added, MR-SNe dominate at low metallicities and it is no longer possible to appreciate differences between different rotational velocities for massive stars. The s-process abundance pattern of the OC sample is well reproduced. The rise in the outer-disc data as well as the peak followed by the decrease in the local and inner disc are reproduced by our model at $R_{GC} = 12, 8,$ and 6 kpc. Only for [Y/Fe] and [Zr/Fe] versus [Fe/H] in the outer region our model predicts a decrease rather than the observed increase, due to too low yields of these elements from LIMS and too high ones from MR-SNe.

(iv) The picture for the mixed-*r*-process elements is more complex. A good agreement with the relevant data is obtained for Mo, even if the model still slightly underestimates the observations, most probably because of the lack of an additional contribution from neutrino-driven SNe. For Nd and Pr, we disagree with Van der Swaelmen et al. (2023), who claim that Nd is characterized by a significant s-process contribution, whereas Pr by a lower one. On the contrary, our model shows a higher production from LIMS of Pr than of Nd. Also in this case, the model underproduces the [Nd/Fe] versus [Fe/H] abundance pattern, while nicely reproduces the [Pr/Fe] versus [Fe/H] one.

As for the abundance gradients, we first compared predictions of our model for the present-day radial gradients of [Fe/H] and [Eu/H] with those traced by GES DR6 OCs with age < 3 Gyr and Cepheids from Luck & Lambert (2011) and Genovali et al. (2015). Then we discussed the evolution with time of the abundance gradients of all the neutron-capture elements studied in this work in comparison with the full OC sample. Our conclusions can be summarized as follows:

(i) The present-day slope of the [Fe/H] gradient predicted by our model is -0.067 ± 0.003 dex kpc⁻¹, slightly steeper both with respect to that of the restricted OC sample and to the one of the Cepheid sample, yet it agrees with other recent slopes of the [Fe/H] gradient from OC samples (Carrera et al. 2019; Donor et al. 2020; Spina et al. 2021, 2022; Zhang et al. 2021).

(ii) The flat slope observed in the OC sample for [Eu/H] is not reproduced by the model in which Eu is produced by a quick and a delayed source (MR-SNe + MNS with a DTD). Models with no delayed source (only with MR-SNe or only with MNS with a constant and short delay time for merging) do not improve the fit to the data. We discussed the possibility of flattening the predicted [Eu/H] gradient by adopting a constant SF efficiency. However, we are not inclined to relax the assumption of a variable SF efficiency, since it has already been proved by many authors (e.g. Colavitti et al. 2009; Spitoni et al. 2015; Grisoni et al. 2018; Palla et al. 2020) that the inside-out scenario by itself is not able to explain the abundance patterns at different Galactocentric distances and the abundance gradients for several elements, as well as the gradient of the SFR and gas density along the thin disc (see Palla et al. 2020). A reasonable explanation for the discrepancy between model results and observations could thus be that clusters with intermediate age ($1 \leq \text{age} \leq 3$ Gyr) are affected by radial migration. In favour of this hypothesis, predictions of our model are much more in agreement with the slopes observed in the inner disc rather than with the outer ones and a better agreement is also obtained with the radial gradients of the Cepheid sample.

(iii) Regarding the time evolution of the [Fe/H] gradient, results of our model for age = 0.5, 2, and 5 Gyr are in agreement with the observed trend if the gradient of the youngest population is computed by removing all giant stars with $\log g < 2.5$ (see M23 for details). In particular, a really limited time evolution of the [Fe/H] gradient between the considered ages should be expected.

(iv) Also for the [Eu/H] gradients, a limited evolution with time is predicted by our model, in agreement with the observations. However, as already seen in the case of the present-day gradient also at different ages, we obtain slopes which are too steep with respect to the observations.

(v) Predictions of our model for the radial [Y/H] and [Zr/H] gradients show a very similar pattern for age = 0.5 and 2 Gyr, in agreement with the OC sample. Also in the case of Ba, La, and Ce, the model predicts an almost identical flat or slightly decreasing pattern for all ages in the inner zone, as observed in the OC sample.

(vi) As for the abundance patterns, also for the radial gradients much more uncertainty is present in reproducing the trend of the other mixed-*r*-process elements. Due to the adopted nucleosynthesis prescriptions, we underestimate the trends for Mo and Nd, and always produce steeper gradients with respect to the observed ones.

(vii) For all the elements belonging to the second s-process peak as well as for Nd and Pr, our model produces a plateau for low Galactocentric distances at all the considered ages. This is most probably due to the effect of LIMS, whose production of those elements reaches an equilibrium value before that in the outer regions, as a consequence of a faster SF.

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DATA AVAILABILITY

The data underlying this article will be shared upon request.

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