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R topics documented:
BergerParker

2 BergerParker

Berg	erParker						Be	erg	zei	r-1	Pai	rk	er	's i	di	vei	rsi	ity	in	ıde	ех															
Index																																				15
	Shannon .	•	•	•	•	•		•	•	•	•	•	•	•		•	•	•	•	•	•	•	 •	•	•	•	 •	•	•	•	•	•	•		•	13
	Renyi																																			
	Rao																																			
	Pielou																																			
	Hill																																			

Berger-Parker's diversity index

Description

Computes Berger-Parker's diversity index on different classes of numeric matrices using a moving window algorithm.

Usage

BergerParker(x, window=3, np=1, na.tolerance=1, cluster.type="SOCK", debugging=FALSE)

Arguments

x	input data may be a matrix, a Spatial Grid Data Frame, a RasterLayer or a list of these objects. In the latter case, only the first element of the list will be considered.
window	the side of the square moving window, it must be a odd numeric value greater than 1 to ensure that the target pixel is in the center of the moving window. Default value is 3.
np	the number of processes (cores) which will be spawned. Default value is 1.
na.tolerance	a numeric value $(0.0-1.0)$ which indicates the proportion of NA values that will be tolerated to calculate Rao's index in each moving window over x . If the relative proportion of NA's in a moving window is bigger than na.tolerance, then the value of the window will be set as NA, otherwise Rao's index will be calculated considering the non-NA values. Default values is 0.0 (i.e., no tolerance for NA's).
cluster.type	the type of cluster which will be created. The options are "MPI" (calls "makeM-PIcluster"), "FORK" and "SOCK" (call "makeCluster"). Default type is "SOCK".
debugging	a boolean variable set to FALSE by default. If TRUE, additional messages will be printed. For de-bugging only.

Details

Berger-Parker's index is the relative abundance of the most abundant category (i.e., unique numerical values in the considered numerical matrix). Berger-Parker's index equals the logarithm of the inverse Renyi's index of order infinity, $log(1/^{\infty}H)$ or the inverse of Hill's index of order infinity, $1/^{\infty}D$.

copNDVI 3

Value

A numerical matrix with dimension as dim(x).

Note

Linux users need to install libopenmpi for MPI parallel computing. Linux Ubuntu users may try: apt-get update; apt-get upgrade; apt-get install mpi; apt-get install libopenmpi-dev; apt-get install r-cran-rmpi

Microsoft Windows users may need some additional work to use "MPI", see: https://bioinfomagician.wordpress.com/2013/11/18/installing-rmpi-mpi-for-r-on-mac-and-windows/

Author(s)

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```

References

Berger, W.H., Parker, F.L. (1970). Diversity of planktonic foraminifera in deep-sea sediments". Science, 168: 1345-1347.

Examples

```
#Minimal example; compute Renyi's index with alpha 1:5
a <- matrix(c(10,10,10,20,20,20,20,30,30),ncol=3,nrow=3)
berpar <- BergerParker(x=a,window=3)</pre>
```

copNDVI

Copernicus Long Term (1999-2017) NDVI Overview (5km)

Description

A RasterLayer (EPSG: 4326) of the global average NDVI value per pixel for the 21st of June over the period 1999-2017.

Usage

copNDVI

Format

RasterLayer:

NDVI Normalised Difference Vegetation Index value (0-255) for each 5 km pixel.

4 CRE

References

https://land.copernicus.eu/global/products/ndvi

CRE

Cumulative Residual Entropy (CRE)

Description

Computes Cumulative Residual Entropy (CRE) on different classes of numeric matrices using a moving window algorithm.

Usage

```
CRE(x, window=9, mode="classic", rescale=FALSE,
na.tolerance=0.0, simplify=3, np=1,
cluster.type="SOCK", debugging=FALSE)
```

Arguments

Х	input data may be a matrix, a Spatial Grid Data Frame, a RasterLayer or a list of these objects. In the latter case, if <i>mode="classic"</i> only the first element of the list will be considered.
window	the side of the square moving window, it must be a odd numeric value greater than 1 to ensure that the target pixel is in the center of the moving window. Default value is 3.
mode	currently, there are two modes to calculate Cumulative Residual Entropy (CRE). If mode is "classic", then the monodimension CRE will be calculated on one single matrix. If mode is "multidimension" (experimental!) a list of matrices must be provided as input. In this latter case, the multidimensional cumulative residual probability will be calculated. Default value is "classic".
rescale	a boolean variable set to FALSE by default. If TRUE, <i>x</i> will be scaled and centered to standardise different matrices if mode is "multidimension". Default value is FALSE.
na.tolerance	a numeric value $(0.0-1.0)$ which indicates the proportion of NA values that will be tolerated to calculate CRE in each moving window over x . If the relative proportion of NA's in a moving window is bigger than na.tolerance, then the value of the window will be set as NA, otherwise CRE will be calculated considering the non-NA values. Default values is 0.0 (i.e., no tolerance for NA's).
simplify	Number of decimal places to be retained to calculate CRE. Only if <i>x</i> is floats.
np	the number of processes (cores) which will be spawned. Default value is 1.
cluster.type	the type of cluster which will be created. The options are "MPI" (which calls "makeMPIcluster"), "FORK" and "SOCK" (which call "makeCluster"). Default type is "SOCK".
debugging	a boolean variable set to FALSE by default. If TRUE, additional messages will be printed. For debugging only.

Hill 5

Details

Unidimension Cumulative Residual Entropy (CRE) is calculated on a numerical vector as $CRE = CRE = -\sum_{i=1}^{N} P(X \ge x_i) \log P(X \ge x_i) dx$ [1] where $dx = (x_i - x_{i-1})$ and P is a vector of probabilities that the vector of observations is larger or equal to each value of the vector. In the "multidimension" CRE, P becomes an array with as many dimensions as the one of the observations. In each cell of P the probability estimates with the frequency of the number of observation that as the same time satisify the larger or equal requirment for the different combination of values along the dimension. dx becomes the products of the difference along each dimension.

The theoretical minimum of CRE is 0, when all values are identical in a window. The values of CRE increases with the range of observations, thus the more the observations are equally spread (even) across values the higher CRE will be.

Value

A matrix of dimension dim(x).

Author(s)

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References

[1] Rao M, Chen Y, Vemuri BC, Wang F (2004) Cumulative Residual Entropy: A New Measure of Information. IEEE Trans Inf Theory 50:1220–1228.

Examples

```
#Minimum example; compute CRE
a <- matrix(c(10,10,10,20,20,20,20,30,30),ncol=3,nrow=3)
out <- CRE(x=a,window=3,na.tolerance=0,mode="classic")

#Minimum example; compute CRE in paralllel
a <- matrix(c(10,10,10,20,20,20,20,30,30),ncol=3,nrow=3)
out <- CRE(x=a,window=3,na.tolerance=0,mode="classic",np=1)

#Compute multidimension Rao's index rescaling the input matrices
a <- matrix(c(10,10,10,20,20,20,20,30,30),ncol=3,nrow=3)
b <- matrix(c(0.5,0.5,0.1,0.1,0.3,0.3,0.3,0.3,0.3),ncol=3,nrow=3)
out <- CRE(x=list(a,b),window=3,na.tolerance=0,
    mode="multidimension",rescale=TRUE,debugging=TRUE)</pre>
```

Hill

Hill's index of diversity - Hill numbers (D)

Description

Computes Hill's index of diversity (Hill numbers) on different classes of numeric matrices using a moving window algorithm.

6 Hill

Usage

```
Hill(x, window = 3, alpha = 1, np = 1, na.tolerance=1,
  cluster.type = "SOCK", debugging = FALSE)
```

Arguments

Х	input data may be a matrix, a Spatial Grid Data Frame, a RasterLayer or a list of these objects. In the latter case, only the first element of the list will be considered.
window	the side of the square moving window, it must be a odd numeric value greater than 1 to ensure that the target pixel is in the center of the moving window. Default value is 3.
alpha	Order of the Hill number to compute the index. If "alpha" is a vector with length greater than 1, then the index will be calculated over x for each value in the sequence.
np	the number of processes (cores) which will be spawned. Default value is 1.
na.tolerance	a numeric value $(0.0-1.0)$ which indicates the proportion of NA values that will be tolerated to calculate Rao's index in each moving window over x . If the relative proportion of NA's in a moving window is bigger than na.tolerance, then the value of the window will be set as NA, otherwise Rao's index will be calculated considering the non-NA values. Default values is 0.0 (i.e., no tolerance for NA's).

cluster.type the type of cluster which will be created. The options are "MPI" (calls "makeM-

PIcluster"), "FORK" and "SOCK" (call "makeCluster"). Default type is "SOCK".

debugging a boolean variable set to FALSE by default. If TRUE, additional messages will

be printed. For debugging only.

Details

Hill numbers (^qD) are calculated on a numerical matrices as $^qD = (\sum_{i=1}^R p^q_{\ i})^{1/(1-q)}$, where q is the order of the Hill number, R is the total number of categories (i.e., unique numerical values in a numerical matrix), p is the relative abundance of each category. When q=1, Shannon.R is called to calculate $exp(H^1)$ instead of the indefinite 1D . if $q>2*10^9$, BerkgerParker.R is called to calculate $1/^\infty D$. Hill numbers of low order weight more rare categories, whereas Hill numbers of higher order weight more dominant categories.

Value

A list of matrices of dimension dim(x) with length equal to the length of alpha.

Note

Linux users need to install libopenmpi for MPI parallel computing. Linux Ubuntu users may try: apt-get update; apt-get upgrade; apt-get install mpi; apt-get install libopenmpi-dev; apt-get install r-cran-rmpi

Microsoft Windows users may need some additional work to use "MPI", see: https://bioinfomagician.wordpress.com/2013/11/18/installing-rmpi-mpi-for-r-on-mac-and-windows/

Pielou 7

Author(s)

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```

References

Hill, M.O. (1973). Diversity and evenness: a unifying notation and its consequences. Ecology 54, 427-431.

See Also

BergerParker Shannon

Examples

```
#Minimal example; compute Hill's index with alpha 1:5
a <- matrix(c(10,10,10,20,20,20,20,30,30),ncol=3,nrow=3)
hill <- Hill(x=a,window=3,alpha=1:5)</pre>
```

Pielou

Pielou's evenness index (E')

Description

Computes Pielou's evenness index on different classes of numeric matrices using a moving window algorithm.

Usage

```
Pielou(x, window=3, np=1, na.tolerance=1, cluster.type="SOCK",
  debugging=FALSE)
```

Arguments

x	input data may be a matrix, a Spatial Grid Data Frame, a RasterLayer or a list of these objects. In the latter case, only the first element of the list will be considered.
window	the side of the square moving window, it must be a odd numeric value greater than 1 to ensure that the target pixel is in the center of the moving window. Default value is 3.
np	the type of cluster which will be created. The options are "MPI" (calls "makeM-PIcluster"), "FORK" and "SOCK" (call "makeCluster"). Default type is "SOCK".

8 Pielou

na.tolerance a numeric value (0.0 - 1.0) which indicates the proportion of NA values that

will be tolerated to calculate Rao's index in each moving window over *x*. If the relative proportion of NA's in a moving window is bigger than na.tolerance, then the value of the window will be set as NA, otherwise Rao's index will be calculated considering the non-NA values. Default values is 0.0 (i.e., no

tolerance for NA's).

cluster.type the type of cluster which will be created. The options are "MPI" (calls "makeM-

PIcluster"), "FORK" and "SOCK" (call "makeCluster"). Default type is "SOCK".

debugging a boolean variable set to FALSE by default. If TRUE, additional messages will

be printed. For debugging only.

Details

Pielou evenness's index (E') is calculated on a numerical matrix as $E' = \frac{\sum_{i=1}^{R} p_i \times log(p_i)}{log(R)}$, where R is the total number of categories (i.e., unique numerical values in the considered numerical matrix) and p is the relative abundance of each category. Pielou's evenness represents the ratio between the observed value of Shannon's Index and the value of Shannon's Index if all categories (R) had the same relative abundance.

Value

A numerical matrix with dimension as dim(x).

Note

Linux users need to install libopenmpi for MPI parallel computing. Linux Ubuntu users may try: apt-get update; apt-get upgrade; apt-get install mpi; apt-get install libopenmpi-dev; apt-get install r-cran-rmpi

Microsoft Windows users may need some additional work to use "MPI", see: https://bioinfomagician.wordpress.com/2013/11/18/installing-rmpi-mpi-for-r-on-mac-and-windows/

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Duccio Rocchini <duccio.rocchini@unibo.it>

References

Pielou, E.C. (1966). The measurement of diversity in different types of biological collections. Journal of Theoretical Biology, 13: 131-144.

See Also

Shannon

Rao 9

Examples

```
#Minimal example; compute Shannon's index
a <- matrix(c(10,10,10,20,20,20,20,30,30),ncol=3,nrow=3)
renyi <- Pielou(x=a,window=3)</pre>
```

Rao

Rao's index of quadratic entropy (Q)

Description

Computes Rao's index of quadratic entropy (Q) on different classes of numeric matrices using a moving window algorithm.

Usage

```
Rao(x, dist_m="euclidean", window=9, mode="classic", lambda=0,
shannon=FALSE, rescale=FALSE, na.tolerance=0.0, simplify=3,
np=1, cluster.type="SOCK", debugging=FALSE)
```

Arguments

Χ

input data may be a matrix, a Spatial Grid Data Frame, a RasterLayer or a list of these objects. In the latter case, if mode="classic" only the first element of the list will be considered.

dist_m

define the type of distance to be calculated between numerical categories. dist_m can be a character string which defines the name of the distance to derive such as "euclidean". The distance names allowed are the same as for proxy::dist. Alternatively, dist_m can be a function which calculates an user defined distance, (i.e., function(x,y) {return(cos(y-x)-sin(y-x))}) or a matrix of distances. If mode="multidimension" then only "euclidean", "manhattan", "canberra", "minkowski" and "mahalanobis" can be used. Default value is "euclidean".

window

the side of the square moving window, it must be a odd numeric value greater than 1 to ensure that the target pixel is in the center of the moving window. Default value is 3. If proxy::dist is a matrix then the function will assume that this is the distance matrix, and therefore no distance will be derived.

mode

currently, there are two modes to calculate Rao's index. If mode is "classic", then the classic Rao's index will be calculated on one single matrix. If mode is "multidimension" (experimental!) a list of matrices must be provided as input. In this latter case, the overall distance matrix will be calculated in a multi- or hyper-dimensional system by using the measure defined through the function argument dist_m. Each pairwise distance is then multiplied by the inverse of the squared number of pixels in the considered moving window, and the Rao's Q is finally derived by applying a summation. Default value is "classic"

lambda

the value of the lambda of Minkowski's distance. Considered only if dist_m = "minkowski" and mode="multidimension". Default value is 0.

10 Rao

shannon a boolean variable set to FALSE by default. If TRUE, a matrix with Shannon

index will be also calculated. Default value is FALSE.

rescale a boolean variable set to FALSE by default. If TRUE, x will be scaled and

centered to standardise different matrices if mode is "multidimension". Default

value is FALSE.

na. tolerance a numeric value (0.0 - 1.0) which indicates the proportion of NA values that

will be tolerated to calculate Rao's index in each moving window over *x*. If the relative proportion of NA's in a moving window is bigger than na.tolerance, then the value of the window will be set as NA, otherwise Rao's index will be calculated considering the non-NA values. Default values is 0.0 (i.e., no

tolerance for NA's).

simplify Number of decimal places to be retained to calculate distances in Rao's index.

Only if *x* is floats.

np the number of processes (cores) which will be spawned. Default value is 1.

cluster.type the type of cluster which will be created. The options are "MPI" (which calls

"makeMPIcluster"), "FORK" and "SOCK" (which call "makeCluster"). Default

type is "SOCK".

debugging a boolean variable set to FALSE by default. If TRUE, additional messages will

be printed. For debugging only.

Details

Classical Rao's Index (Q) is calculated on a numerical matrix as $Q = \sum_{i=1}^{R} \sum_{j=1}^{R} d_{i,j} \times p_i \times p_j$ [1]. Where R is the number of categories, whereas i and j are pair of numerical categories in the same moving window. In the "multidimension" Rao's index, distances among categories are calculated considering more than one layer, then the pairwise distance between each pair of numerical categories is multiplied to the square of the size of the moving window (which is somewhat the same as to calculate the variance of the multidimensional distance [2].).

The theoretical minimum of Rao's Q is 0, when all categories in a window have distance 0. If the distance chosen to calculate Rao's Index ranges between 0 and 1, the maximum value of Rao's Index equals the Simpson Index of Diversity $1-1/S_i$ where S is the number of categories in window i.

Value

If shannon=TRUE, a list of matrices of length two, otherwise a matrix of dimension dim(x).

Author(s)

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References

[1] Rao, C.R. (1982). Diversity and dissimilarity coefficients: a unified approach. Theoretical Population Biology, 21: 2443. [2] Rocchini, D., M. Marcantonio, and C. Ricotta (2017). Measuring Rao's Q diversity index from remote sensing: An open source solution. Ecological Indicators. 72: 234–238.

Renyi 11

Examples

Renyi

Renyi's entropy (H)

Description

Computes Renyi's entropy $({}^qH)$ on different classes of numeric matrices using a moving window algorithm.

Usage

```
Renyi(x, window=3, alpha=1, base=exp(1), np=1, na.tolerance=1,
cluster.type="SOCK", debugging=FALSE)
```

tolerance for NA's).

Arguments

х	input data may be a matrix, a Spatial Grid Data Frame, a RasterLayer or a list of these objects. In the latter case, only the first element of the list will be considered.
window	the side of the square moving window, it must be a odd numeric value greater than 1 to ensure that the target pixel is in the center of the moving window. Default value is 3.
alpha	Order of diversity to compute the index. If alpha is a vector with length greater than 1, then the index will be calculated over x for each value in the sequence.
base	a numerical value which defines the base of the logarithm in Renyi's entropy formula. Defalut value is exp(1).
np	the number of processes (cores) which will be spawned. Default value is 1.
na.tolerance	a numeric value $(0.0-1.0)$ which indicates the proportion of NA values that will be tolerated to calculate Rao's index in each moving window over x . If the relative proportion of NA's in a moving window is bigger than na.tolerance, then the value of the window will be set as NA, otherwise Rao's index will be calculated considering the non-NA values. Default values is 0.0 (i.e., no

12 Renyi

cluster.type the type of cluster which will be created. The options are "MPI" (calls "makeM-PIcluster"), "FORK" and "SOCK" (call "makeCluster"). Default type is "SOCK".

debugging a boolean variable set to FALSE by default. If TRUE, additional messages will be printed. For debugging only.

Details

Renyi's entropy (^qH) is calculated on a numerical matrix as $^qH=\frac{1}{(1-q)}\ln(\sum_{i=1}^R p^q_i)$, where q is the considered order of diversity (alpha), R is the total number of categories (i.e., unique numerical values in the considered numerical matrix) and p is the relative abundance of each category. If q=1, Shannon.R is called to calculate H' instead of the indefinite 1D , if $p>2*10^9$, then BerkgerParker.R is called to calculate $log(1/^\infty H)$. Renyi's entropy of low order weight more rare numerical categories, whereas values of higher order weight more dominant categories.

Value

A list of matrices with length equal to the length of "alpha". If length of "alpha" is 1, then a matrix of dimension dim(x).

Note

Linux users need to install libopenmpi for MPI parallel computing. Linux Ubuntu users may try: apt-get update; apt-get upgrade; apt-get install mpi; apt-get install libopenmpi-dev; apt-get install r-cran-rmpi

Microsoft Windows users may need some additional work to use "MPI", see: https://bioinfomagician.wordpress.com/2013/11/18/installing-rmpi-mpi-for-r-on-mac-and-windows/

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Duccio Rocchini <duccio.rocchini@unibo.it>
```

References

Rényi, A., 1970. Probability Theory. North Holland Publishing Company, Amsterdam.

See Also

Shannon, BergerParker

Examples

```
#Minimal example; compute Renyi's index with alpha 1:5
a <- matrix(c(10,10,10,20,20,20,30,30),ncol=3,nrow=3)
renyi <- Renyi(x=a,window=3,alpha=1:5)</pre>
```

Shannon 13

Shannon	Shannon's diversity index (H')
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Description

Computes Shannon's diversity index (H') on different classes of numeric matrices using a moving window algorithm.

Usage

Shannon(x, window=3, np=1, na.tolerance=1, cluster.type="SOCK", debugging=FALSE)

Arguments

Х	input data may be a matrix, a Spatial Grid Data Frame, a RasterLayer or a list of these objects. In the latter case, only the first element of the list will be considered.
window	the side of the square moving window, it must be a odd numeric value greater than 1 to ensure that the target pixel is in the center of the moving window. Default value is 3.
np	the number of processes (cores) which will be spawned. Default value is 1.
na.tolerance	a numeric value $(0.0-1.0)$ which indicates the proportion of NA values that will be tolerated to calculate Rao's index in each moving window over x . If the relative proportion of NA's in a moving window is bigger than na.tolerance, then the value of the window will be set as NA, otherwise Rao's index will be calculated considering the non-NA values. Default values is 0.0 (i.e., no tolerance for NA's).
cluster.type	the type of cluster which will be created. The options are "MPI" (calls "makeM-PIcluster"), "FORK" and "SOCK" (call "makeCluster"). Default type is "SOCK".
debugging	a boolean variable set to FALSE by default. If TRUE, additional messages will be printed. For debugging only.

Details

Shannon's index (H') is calculated on a numerical matrix as $H' = \sum_{i=1}^{R} p_i \times log(p_i)$, where R is the total number of categories (i.e., unique numerical values in the considered numerical matrix) and p is the relative abundance of each category.

Value

A numerical matrix with dimension $\{\dim(x)\}$.

14 Shannon

Note

Linux users need to install libopenmpi for MPI parallel computing. Linux Ubuntu users may try: apt-get update; apt-get upgrade; apt-get install mpi; apt-get install libopenmpi-dev; apt-get install r-cran-rmpi

Microsoft Windows users may need some additional work to use "MPI", see: https://bioinfomagician.wordpress.com/2013/11/18/installing-rmpi-mpi-for-r-on-mac-and-windows/

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References

Shannon, C.E. (1948). A mathematical theory of communication. Bell System Technical Journal, 27: 379-423, 623-656.

Examples

```
#Minimal example; compute Shannon's index
a <- matrix(c(10,10,10,20,20,20,20,30,30),ncol=3,nrow=3)
shannon <- Shannon(x=a,window=3)</pre>
```

Index

```
*Topic datasets
    copNDVI, 3
*Topic methods
    BergerParker, 2
    CRE, 4
    Hill, 5
    Pielou, 7
    Rao, 9
    Renyi, 11
    Shannon, 13
BergerParker, 2, 7, 12
copNDVI, 3
CRE, 4
Hill, 5
Pielou, 7
Rao, 9
Renyi, 11
Shannon, 7, 8, 12, 13
```